

PYRAMID WAVEFRONT SENSING IN THE ERA OF EXTREME OPTICS

LAUREN H SCHATZ^{1,2}

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OUTLINE

- Motivation: Exoplanet Imaging
- Extreme Adaptive Optics
 - MagAO-X Update
 - Pyramid Wavefront Sensing
- Three sided Pyramid Wavefront Sensor
 - Operation
 - Mathematics
 - Performance

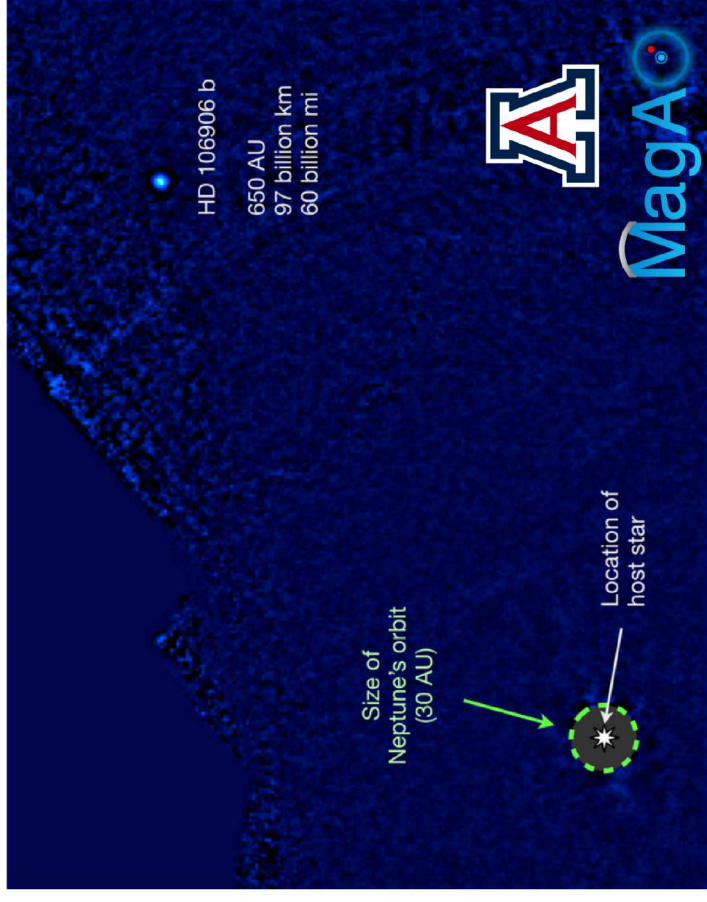
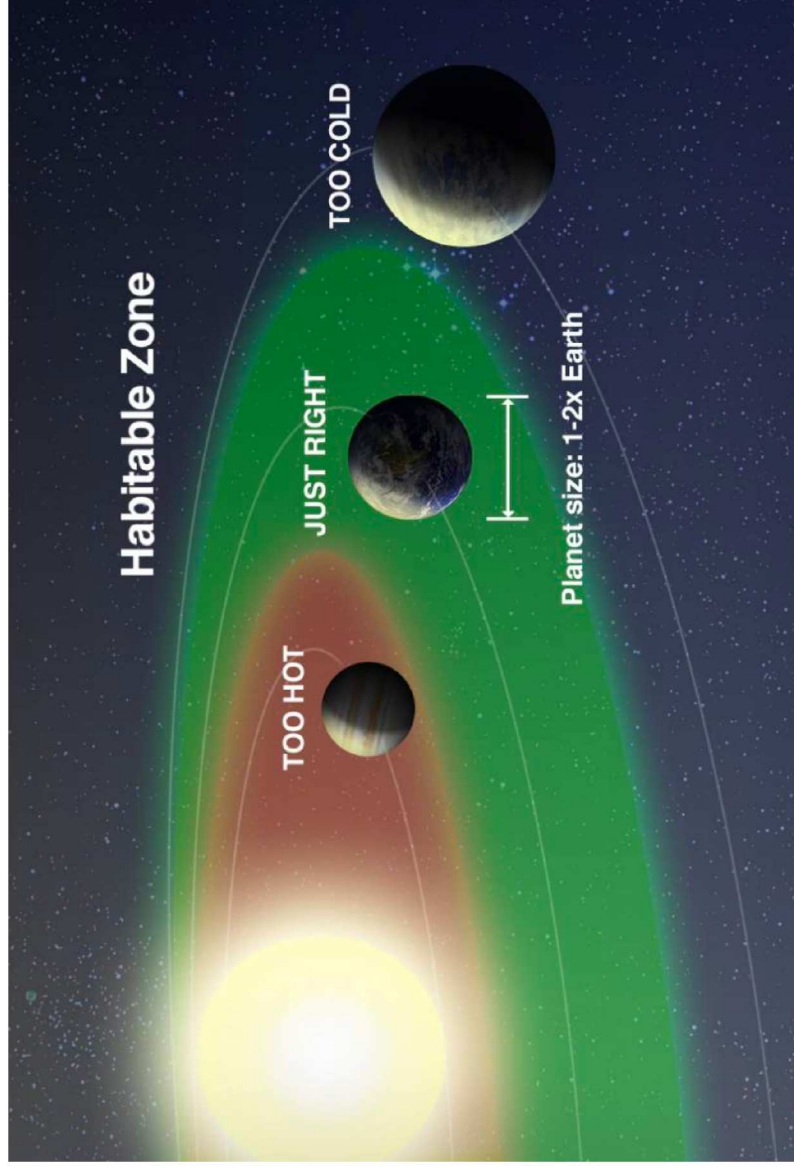


Image Credit, Vanessa Bailey, University of Arizona

THE HABITABLE ZONE

- 4013 exoplanets as of March 21st, 2019
- Region around a star where a planet can support liquid water.
- Earth sized planets in this region are potentially habitable



A TINY BLUE DOT

- Image of Earth from Cassini Space Craft
- How do we characterize a tiny blue dot?

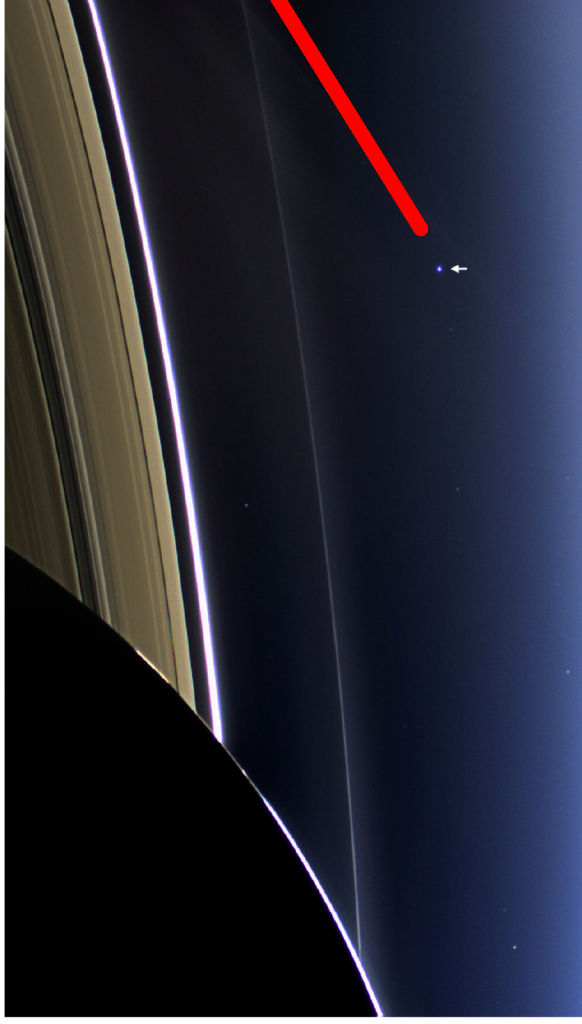


Image credit: NASA Cassini Mission

Motivation

SOME PROBLEMS: CONTRAST AND TURBULENCE



Contrast

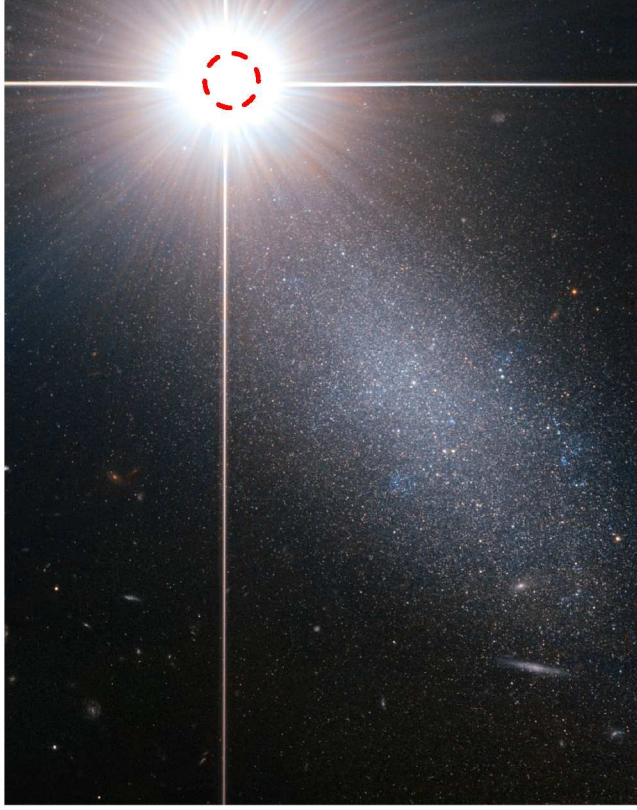


Photo Credit: NASA Hubble Space Telescope

Atmospheric Turbulence

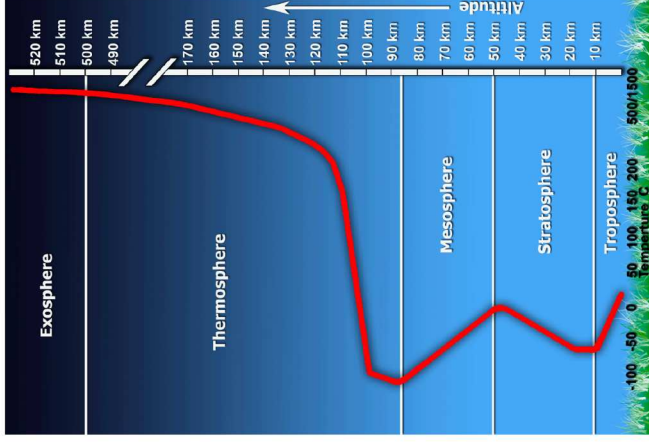
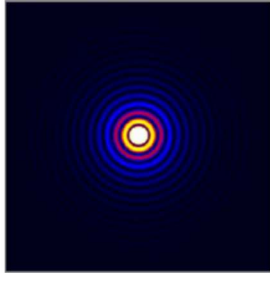
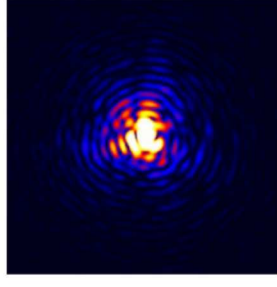


Image Credit: NASA Climate Science Investigations



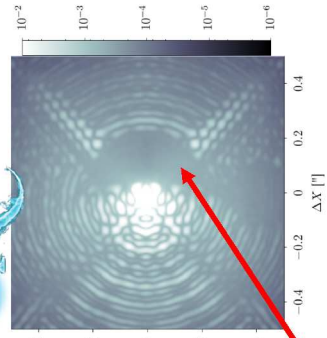
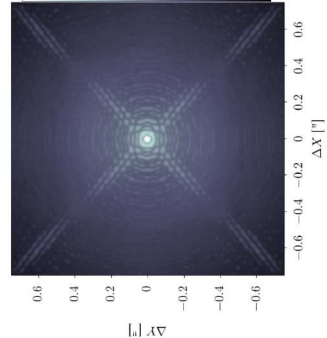
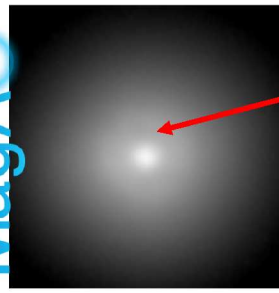
Star without turbulence



Star with turbulence

Motivation

DIRECT IMAGING OF EXOPLANETS



c/o Kate Follette

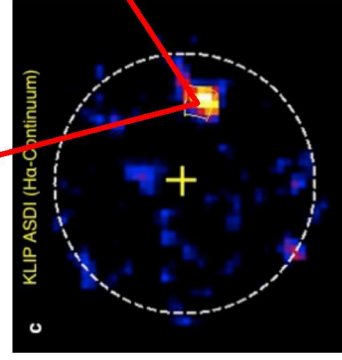
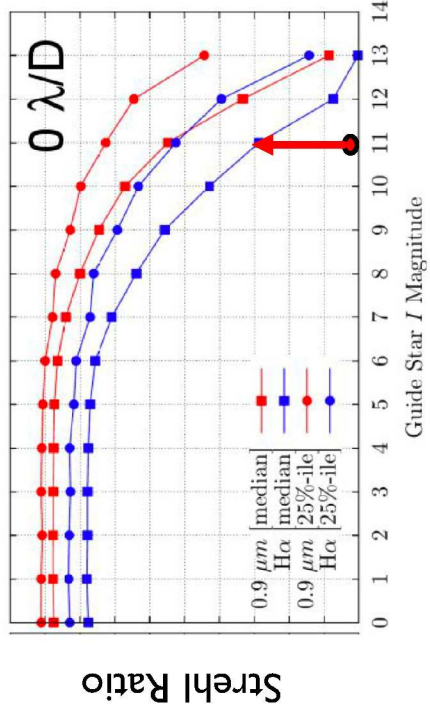
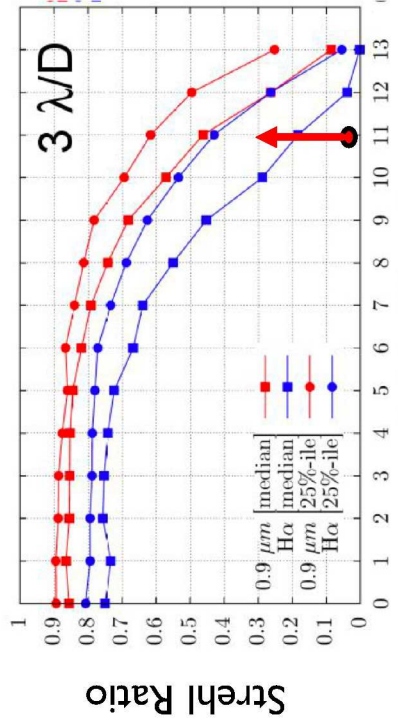
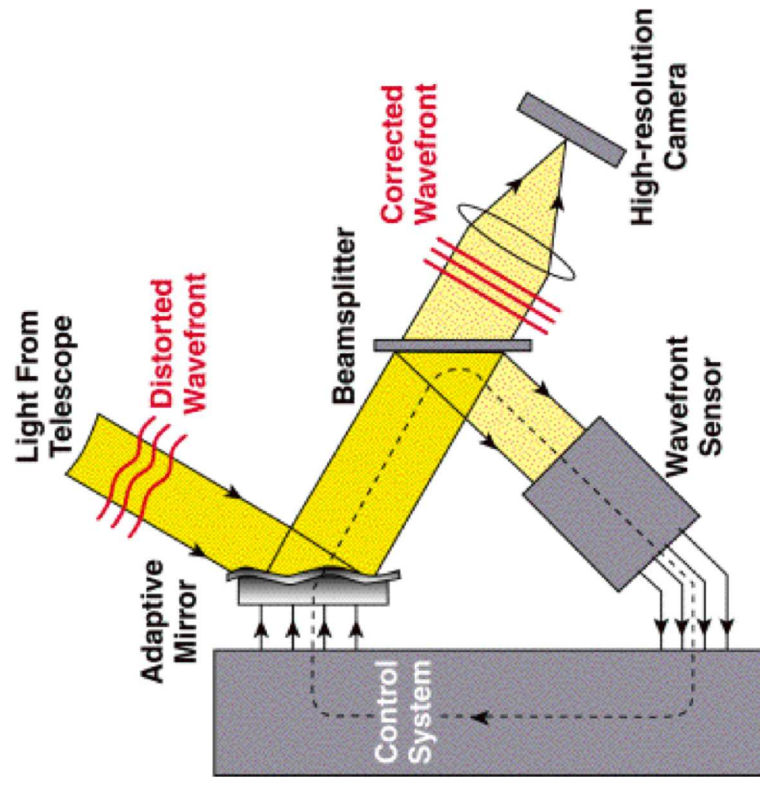


Image of LkCa 15b taken by Kate Follette (Sallum et al., Nature, 2015)

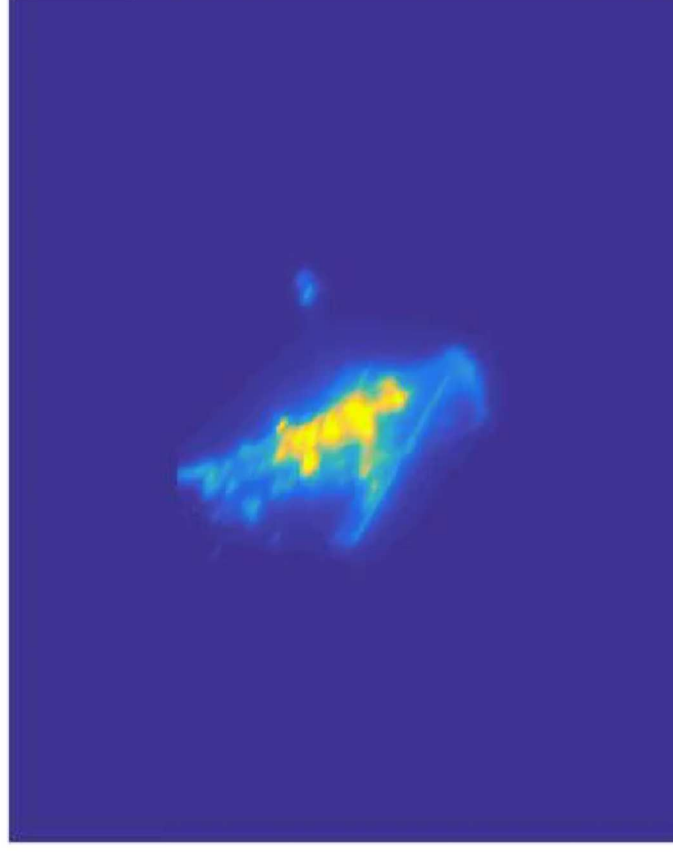
High airmass and 11th mag GS demand high performance.



ADAPTIVE OPTICS



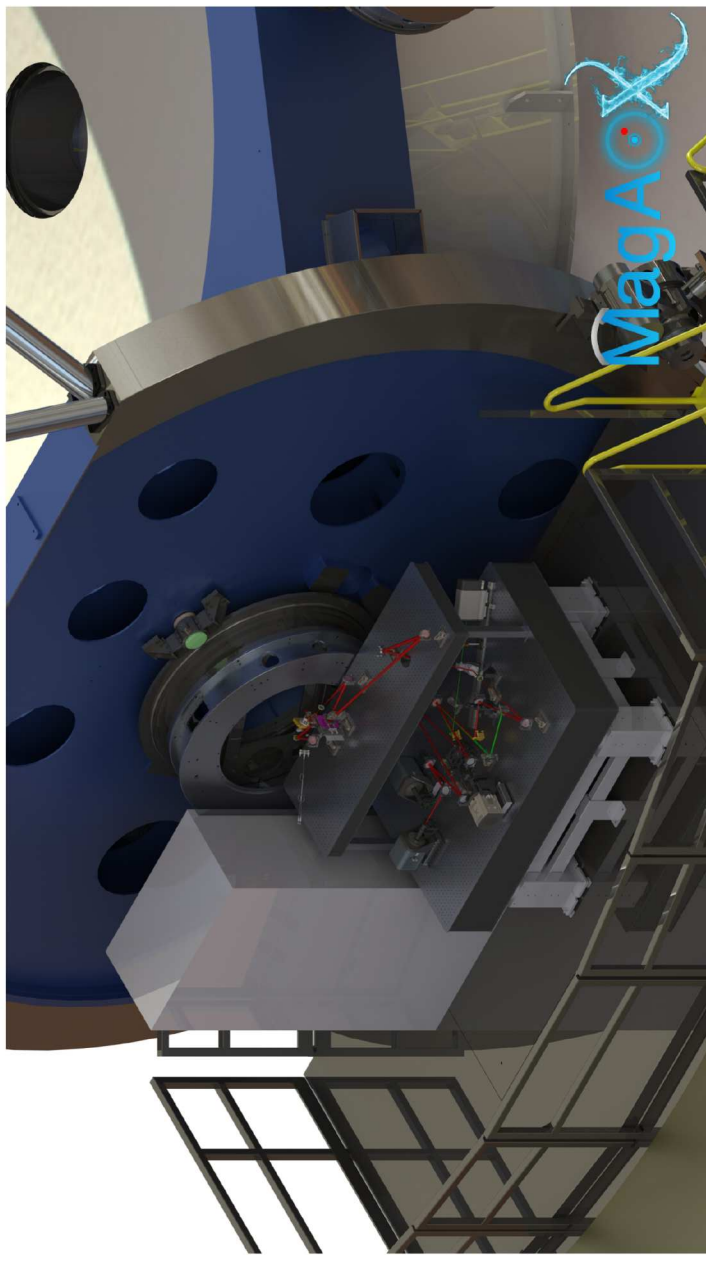
Hubble with AO on/off



EXTREME AO: ONE STEP FURTHER



- Key Components:
- Deformable Mirror with high actuator count
 - High performance wavefront sensor
 - High contrast coronagraph



Extreme AO

EXTREME AO: ONE STEP FURTHER

MagAOX

- Key Components:
- Deformable Mirror with high actuator count
 - High performance wavefront sensor
 - High contrast coronagraph

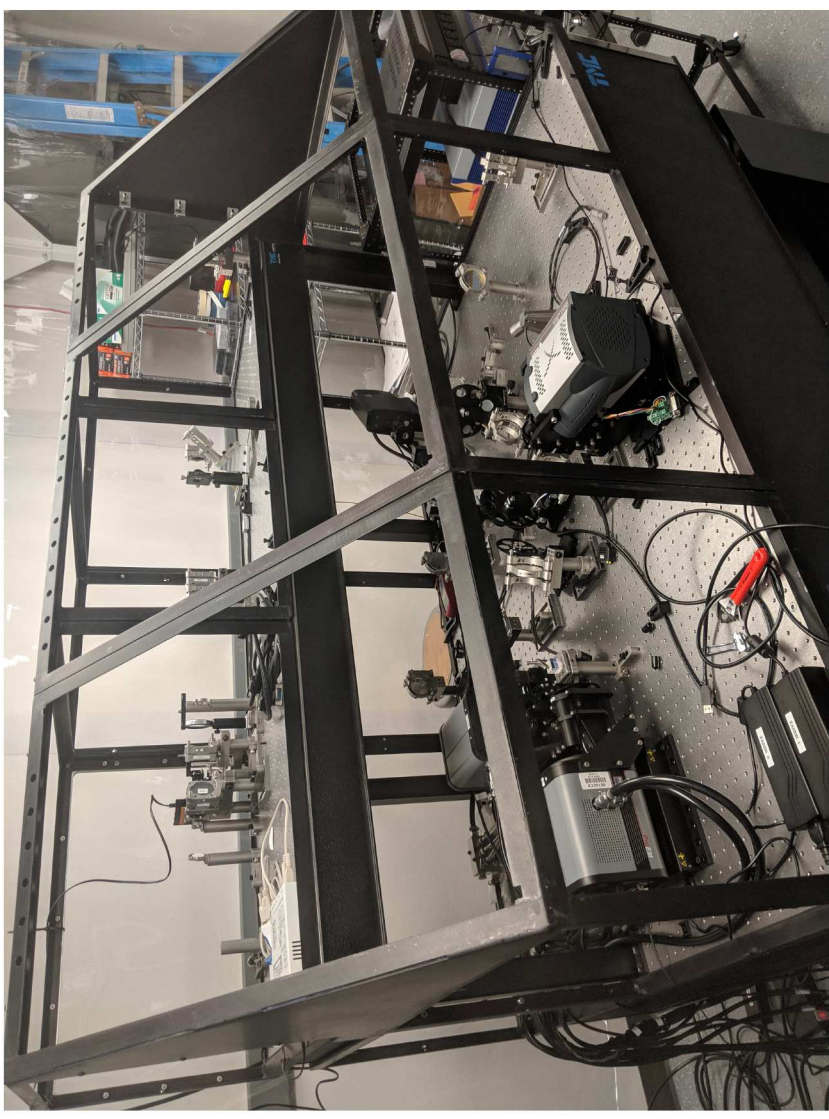


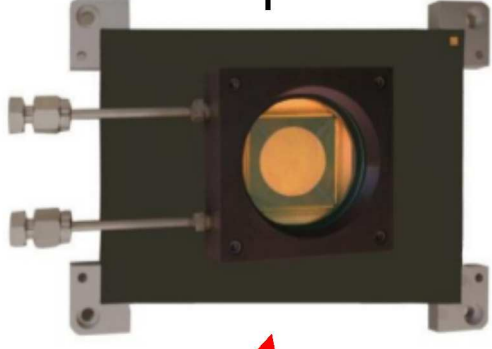
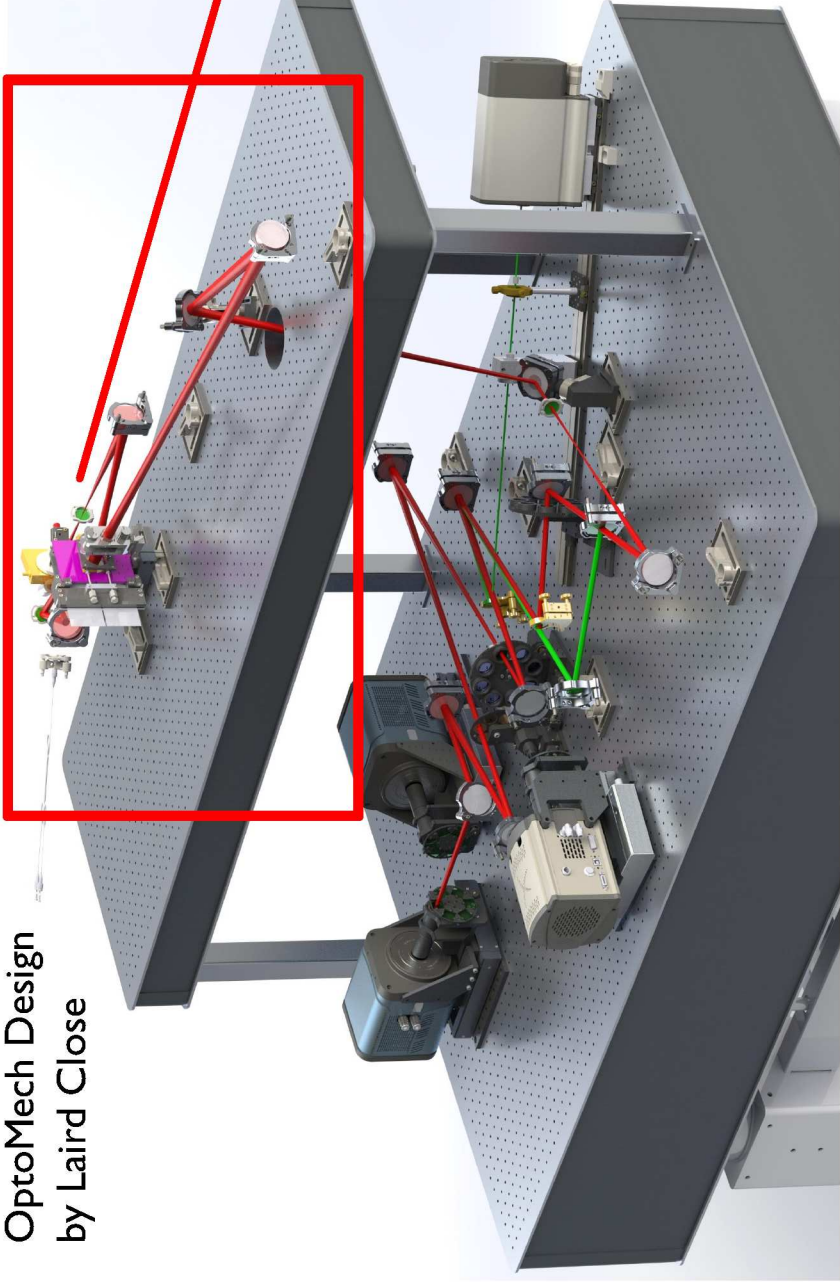
Photo Credit: Jared Males

Extreme AO

MAGAO-X: DEFORMABLE MIRROR



OptoMech Design
by Laird Close



BMC 2K
Tweeter DM



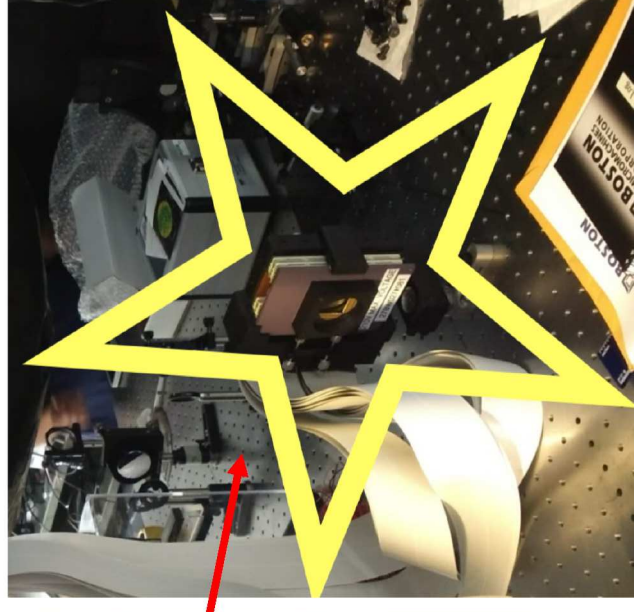
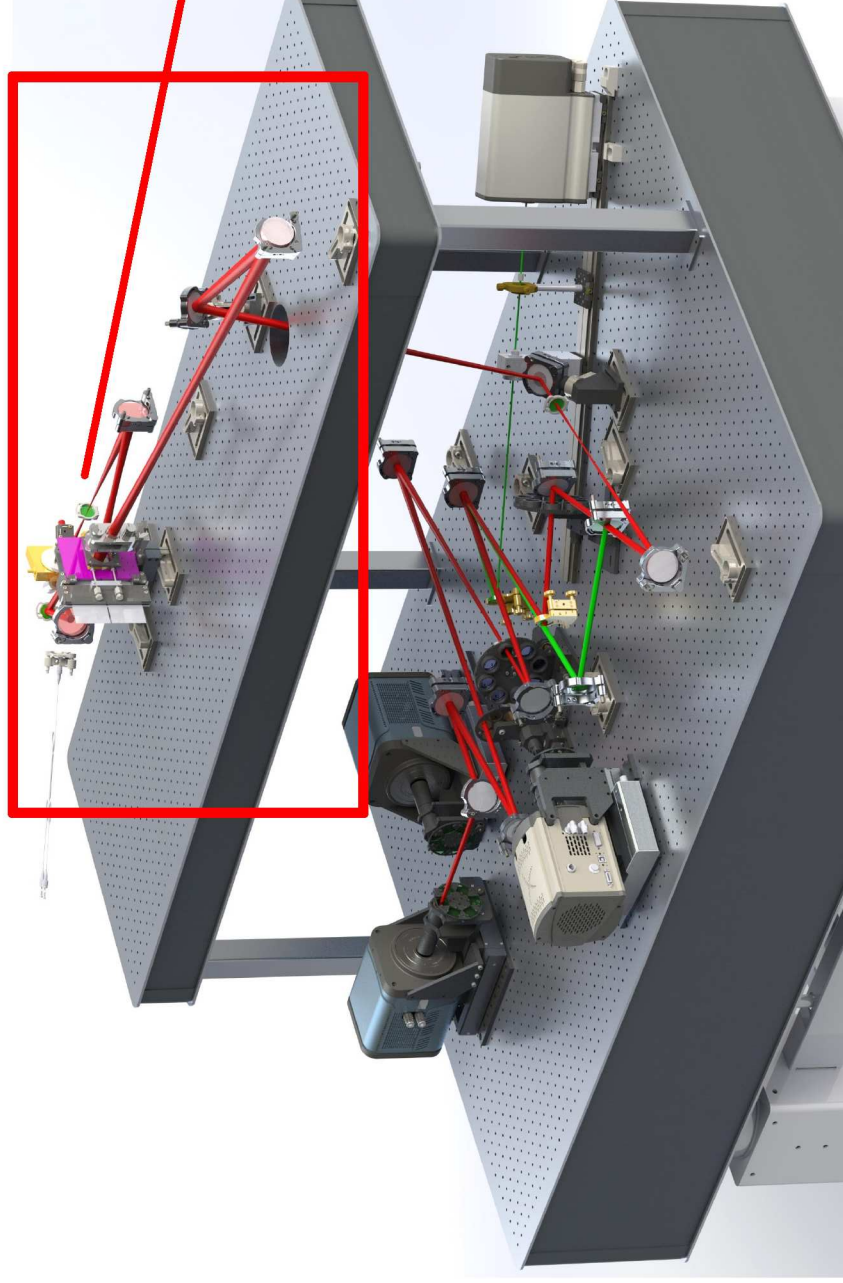
585 actuators



2048 actuators

Extreme AO

MAGAO-X: DEFORMABLE MIRROR

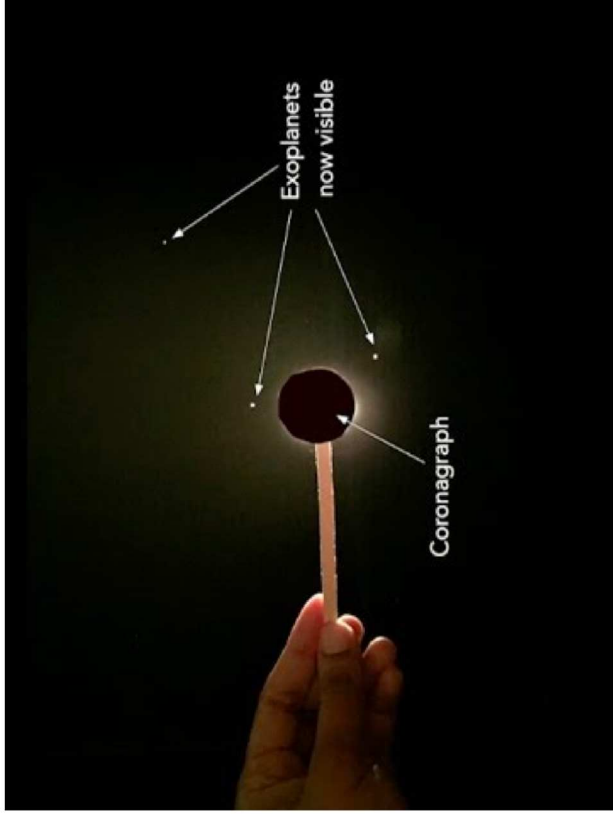


BMC 2K

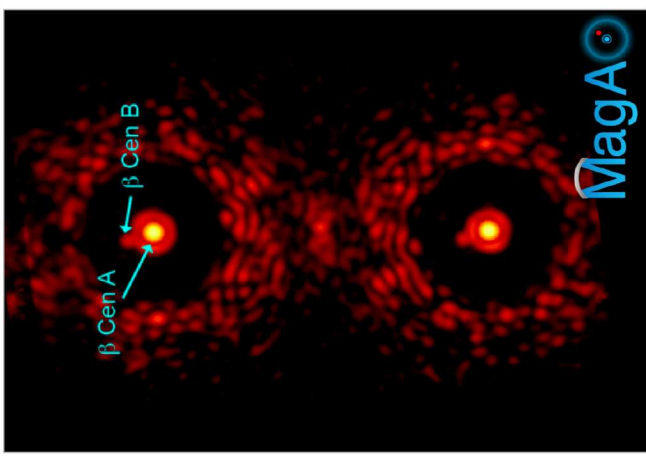
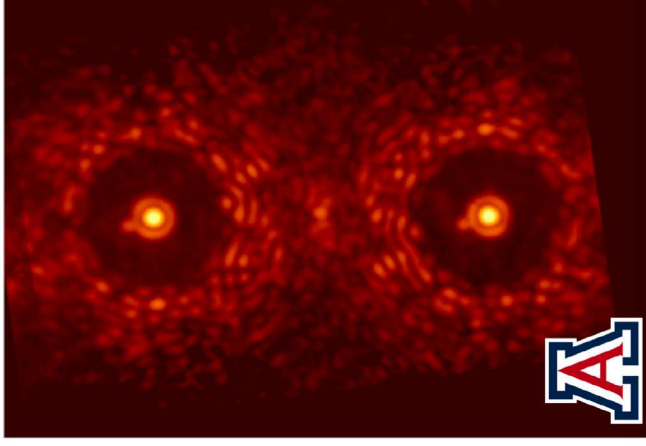
Tweeter DM

Photo Credit: Kyle Van Gorkom

CORONAGRAPHS



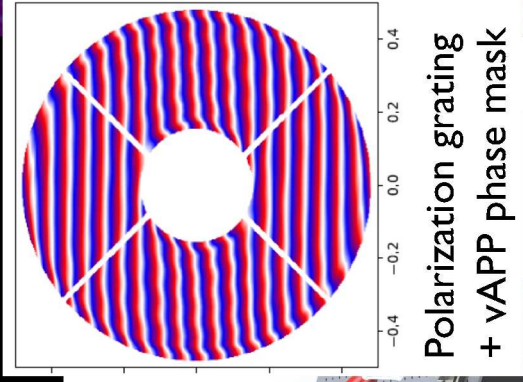
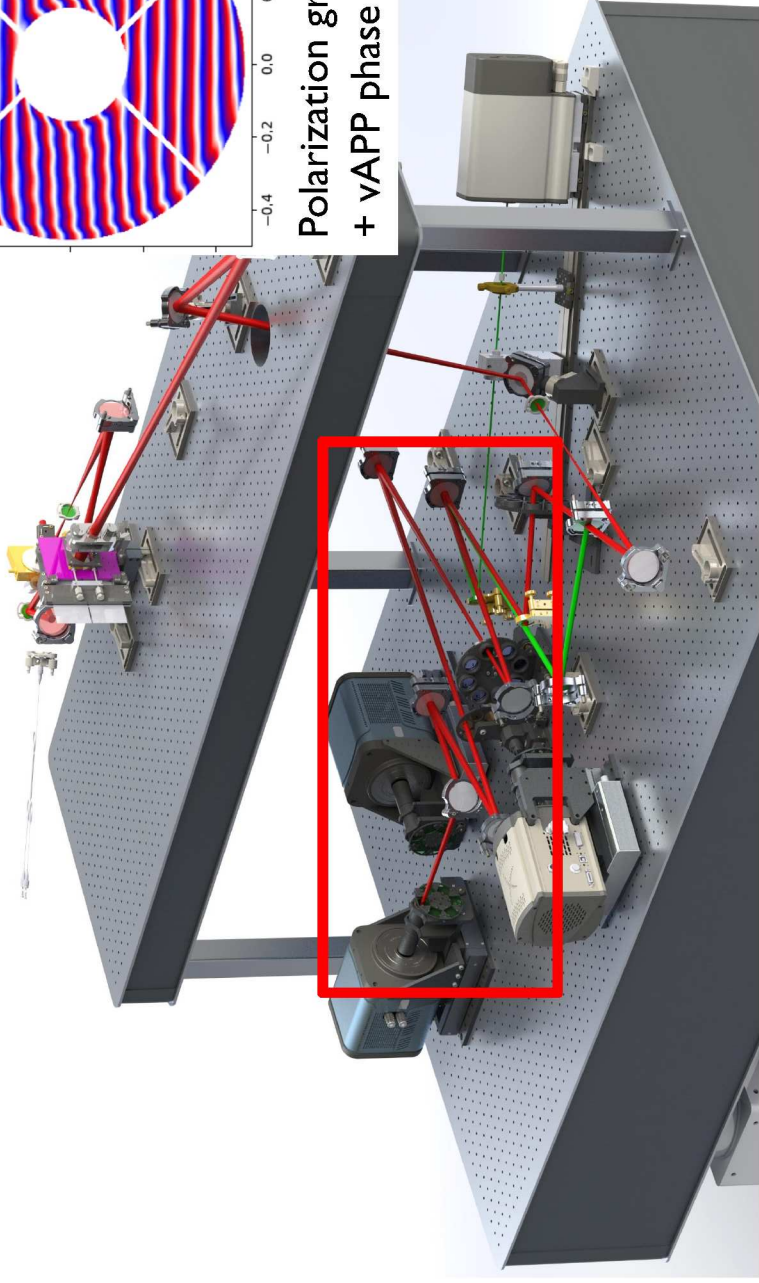
At it's simplest:A dark spot to block the star



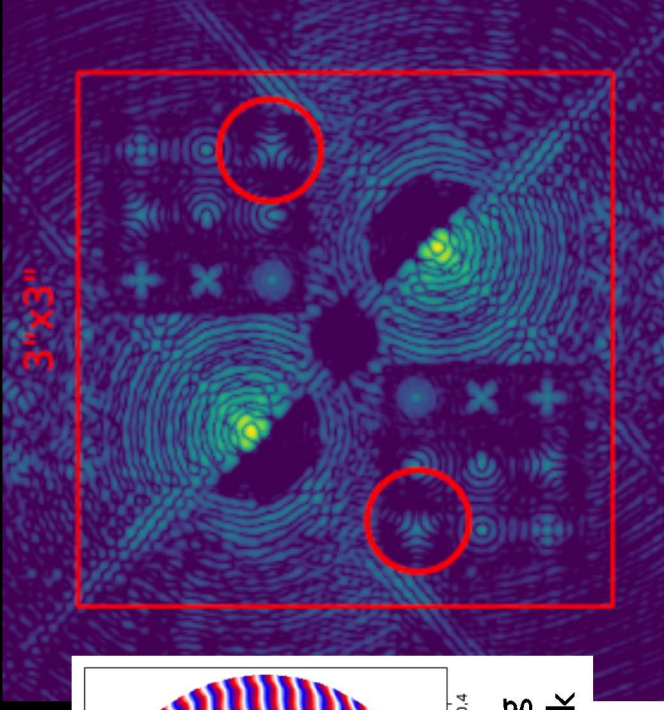
Double image of the star beta Centauri taken through an experimental version of the vector-APP coronagraph installed at MagAO. Binary Companion easily seen. Credit Leiden University, University of Arizona.

Extreme AO

MAGAO-X: CORONAGRAPH



Polarization grating
+ vAPP phase mask



MagAO

vAPP coronagraph

MagAOX

vAPP +
Focal plane
wavefront sensing

vAPP Designed and Manufactured by Univ. of Leiden

Extreme AO

MAGAO-X: CORONAGRAPH

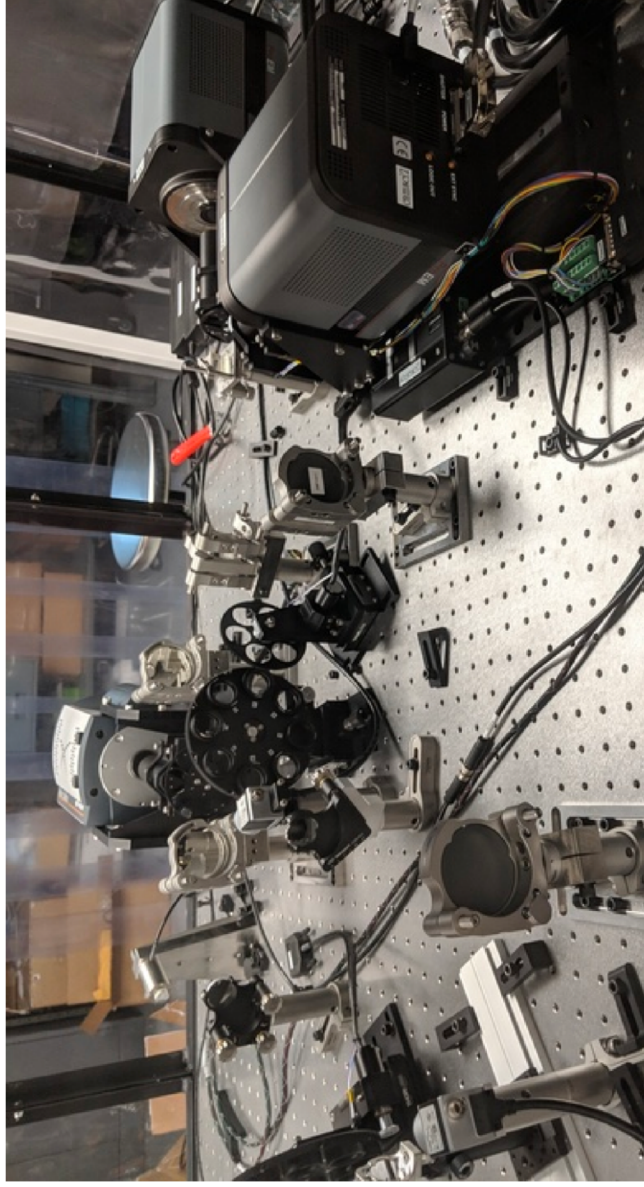
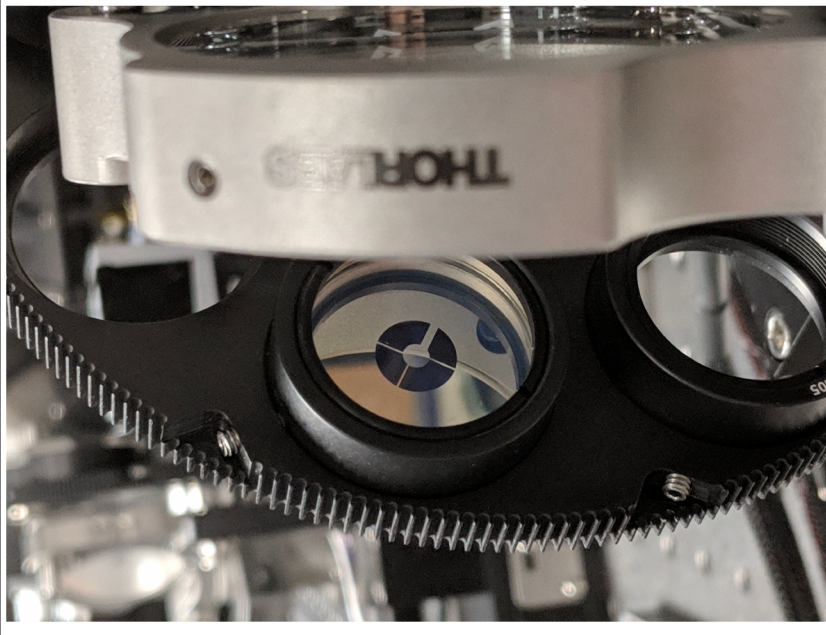
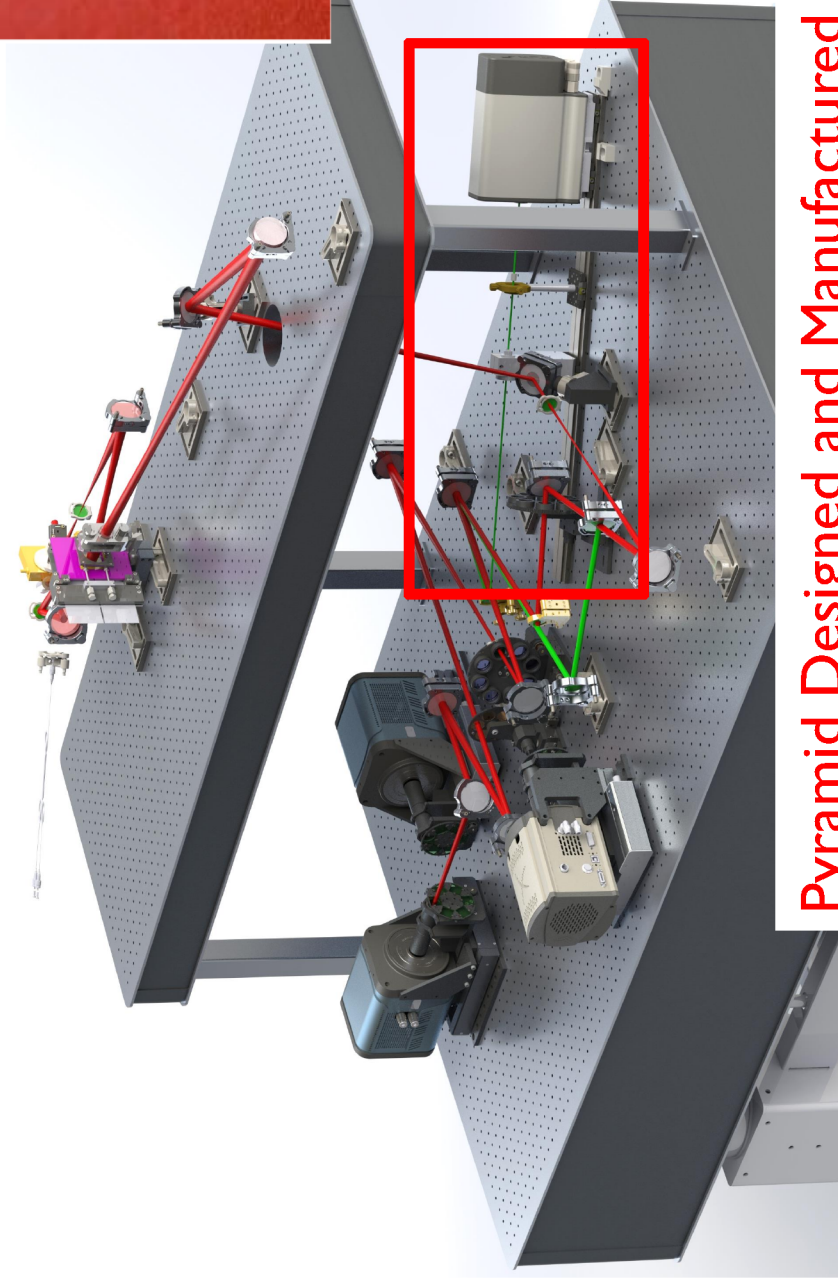
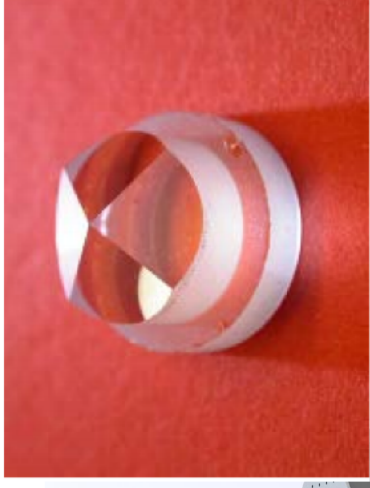


Photo Credit: Jared Males

Extreme AO

MAGAO-X: PYRAMID WAVEFRONT SENSOR



MagAO

Pyramid

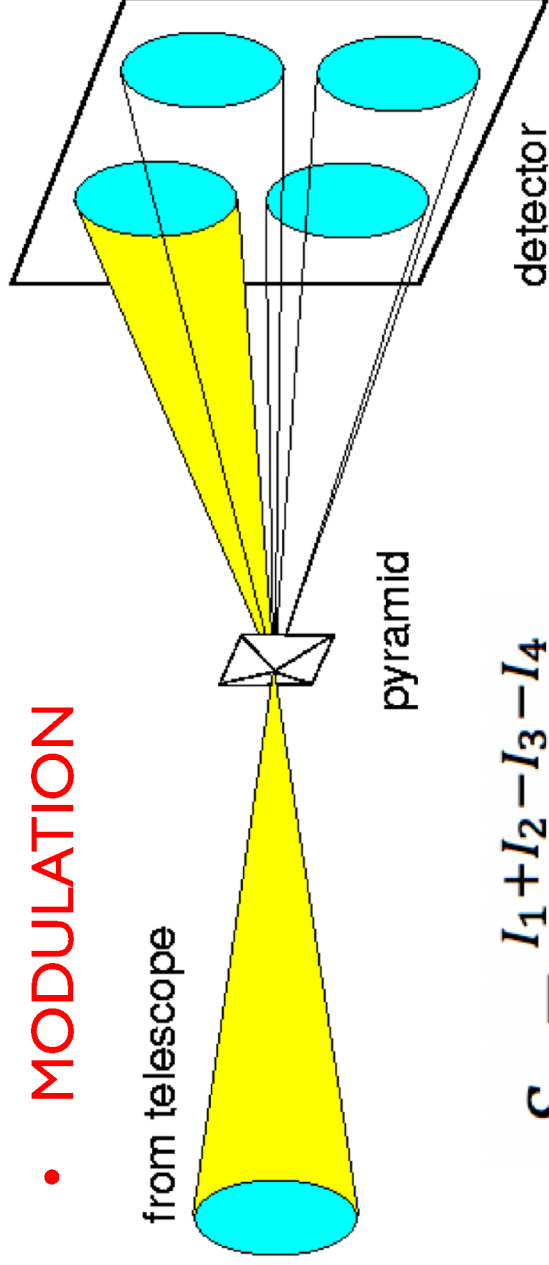
MagAO

Pyramid+OCAM2K

Pyramid Designed and Manufactured by Arcetri

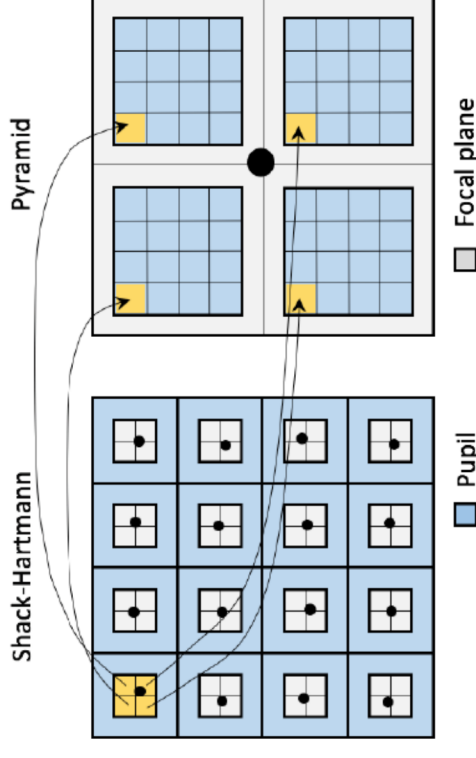
PYRAMID WAVEFRONT SENSING

- MODULATION



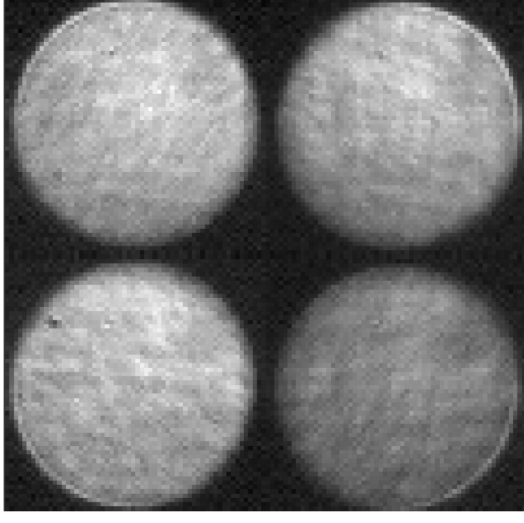
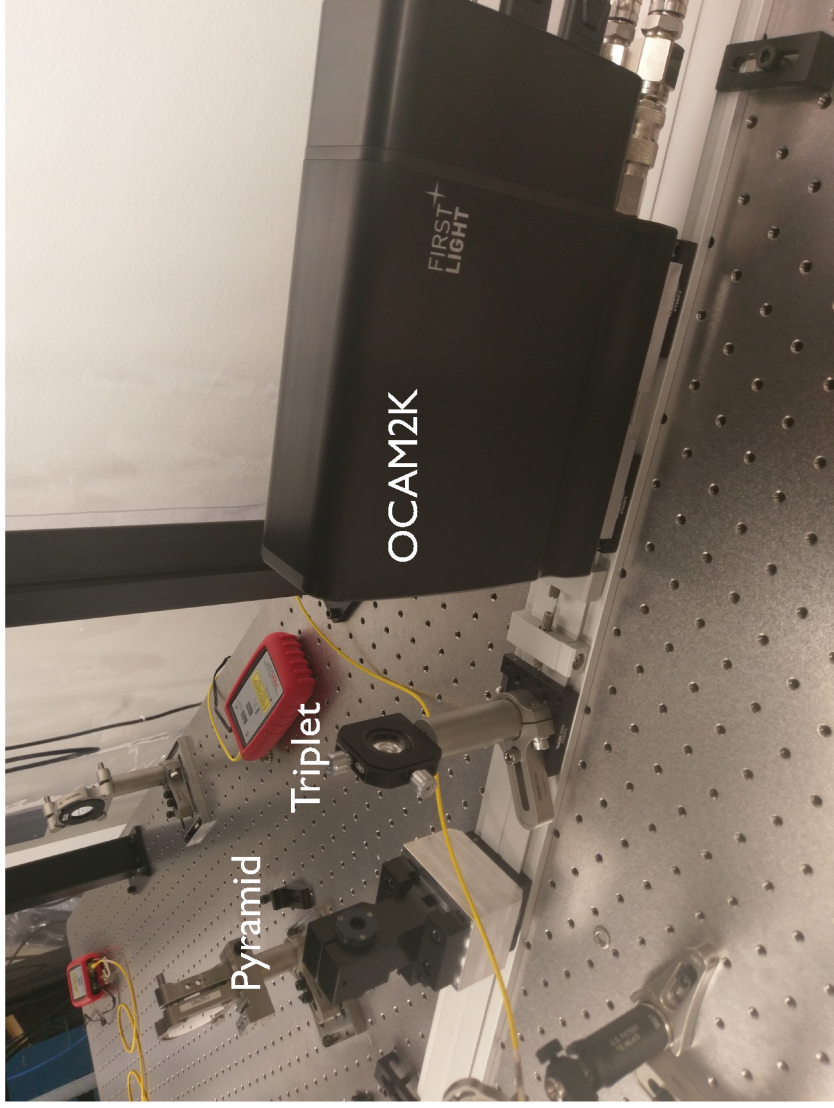
$$S_x = \frac{I_1 + I_2 - I_3 - I_4}{I_1 + I_2 + I_3 + I_4}$$

$$S_y = \frac{I_1 - I_2 - I_3 + I_4}{I_1 + I_2 + I_3 + I_4}$$



of pixels = # of degrees of freedom controlled

MAGAO-X: PYRAMID WAVEFRONT SENSOR



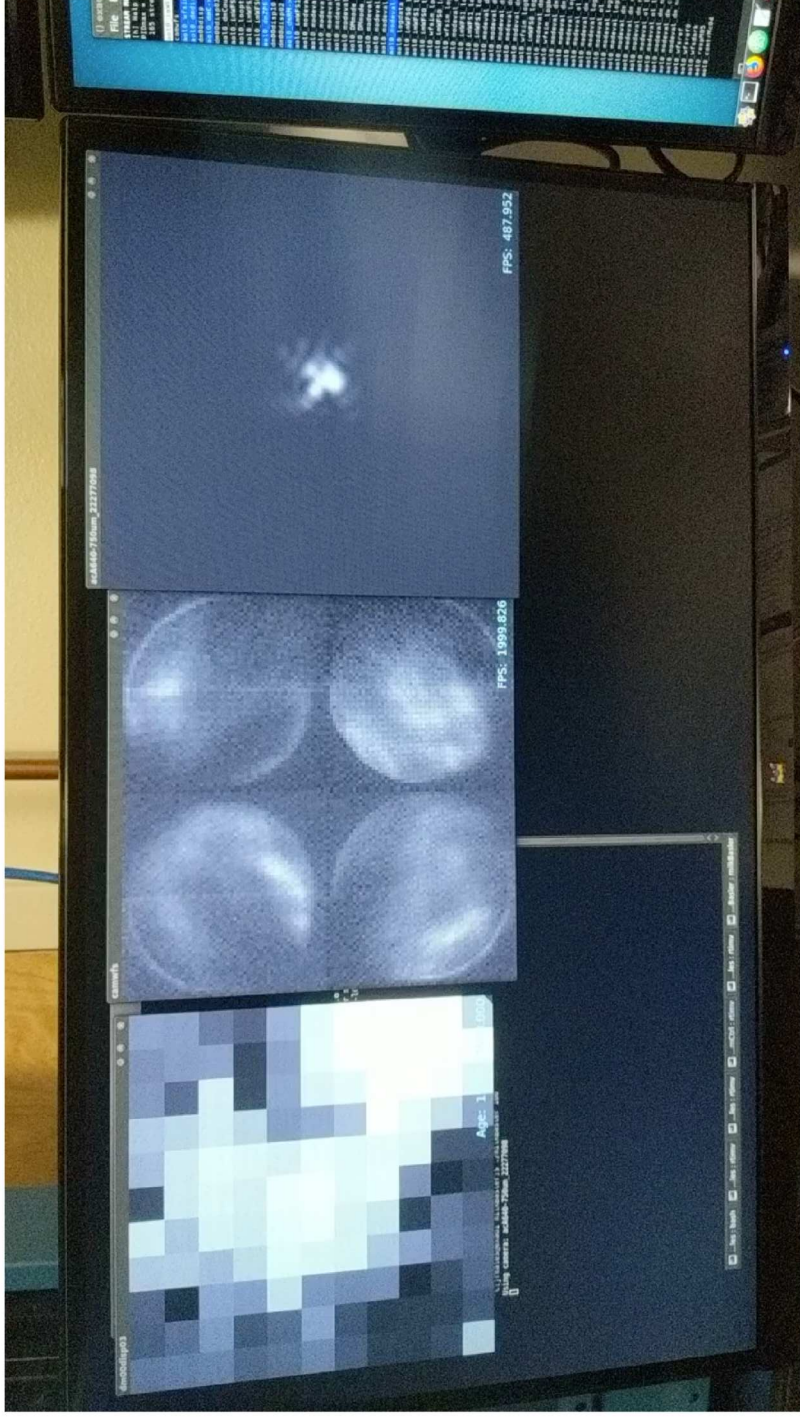
MagAO

Pyramid 32x32

MagAO-X

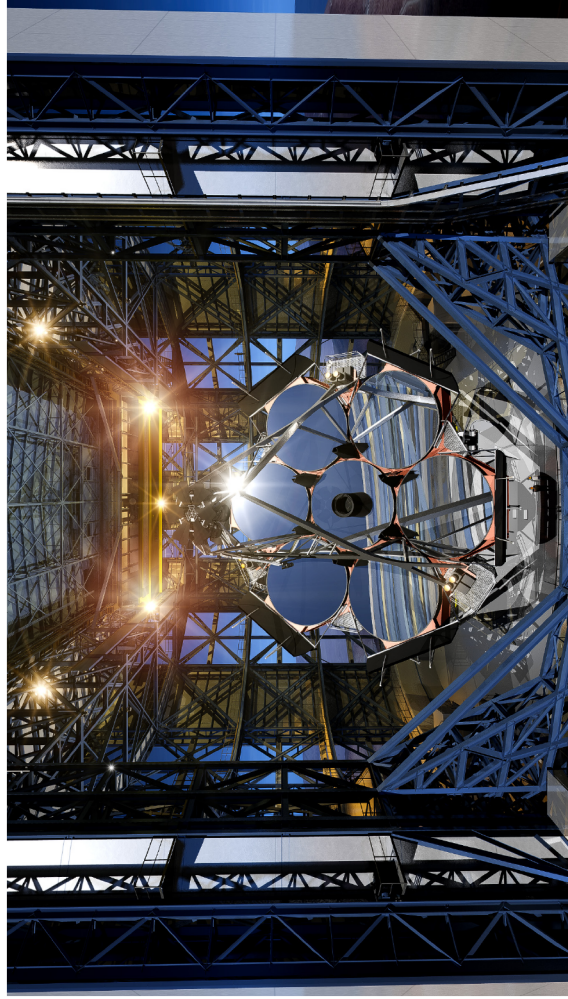
Pyramid+OCAM2K
56x56

CLOSED LOOP!



- 2 kHz speed!
- Goal is 3.6kHz

THE EXTREMELY LARGE TELESCOPES



Artist rendering of the Giant Magellan Telescope (GMT).

7 mirrors make up the primary

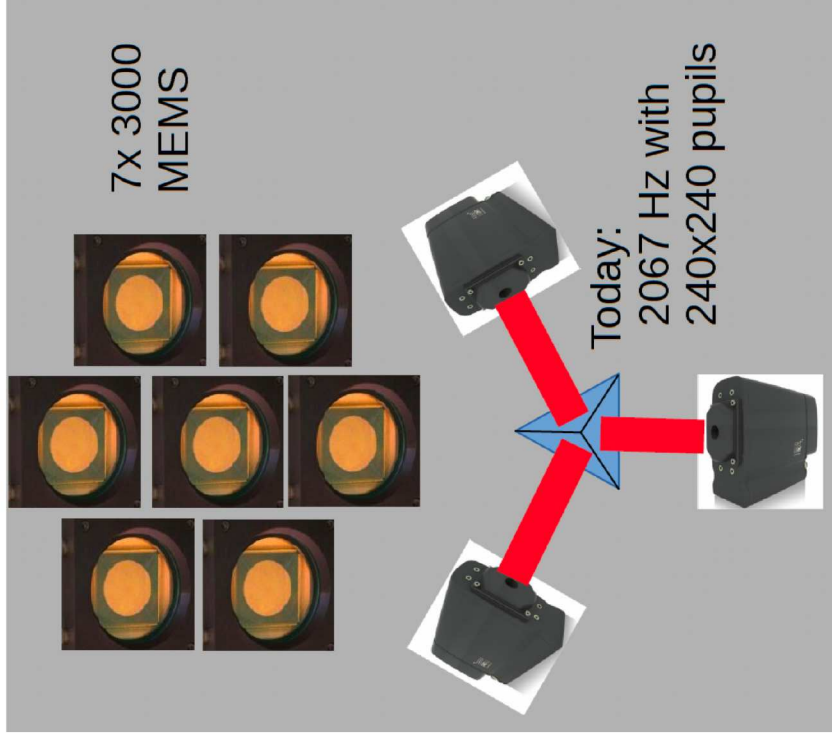
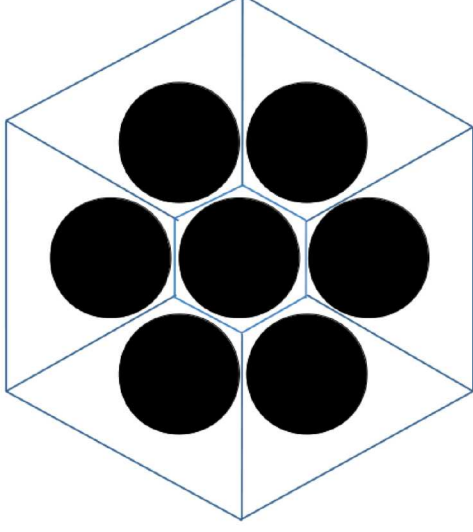


Artist rendering of the Extremely Large Telescope (ELT).



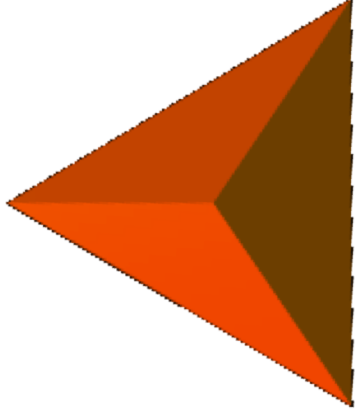
THE GIANT MAGELLAN TELESCOPE EXTREME ADAPTIVE OPTICS SYSTEM: GMAGAO-X

- 7x 3,000 actuator deformable mirrors
- 3 OCAM2K detectors
- 240 x 240 mode 2kHz on OCAM2k



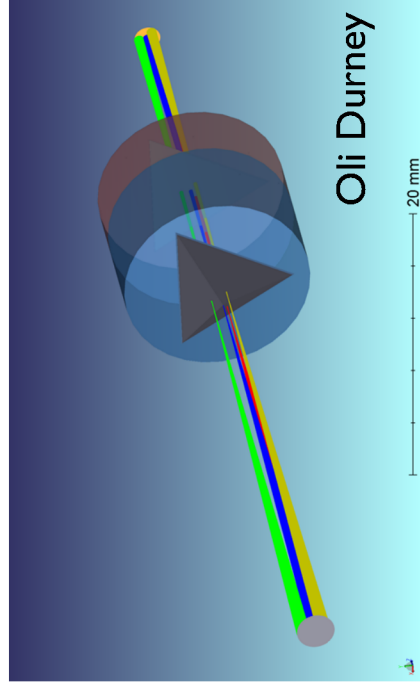
THE 'THREE' AMID WAVEFRONT SENSOR

- Starting with a refractive 3PWFS
- How to treat the wavefront sensor signals
- Sensitivity
- Overall Performance



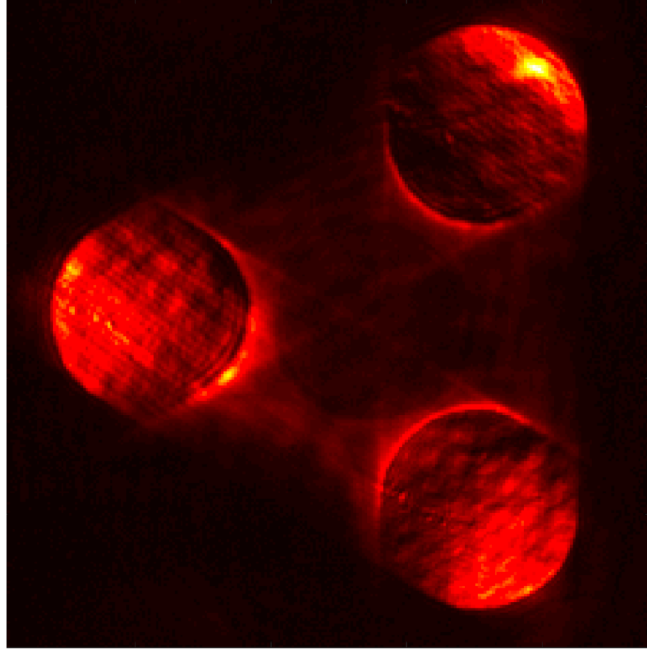
Some Benefits:

- Easier to Manufacture
- Less pixels=less sensitive to read noise
- Simpler than a reflective 4PWFS

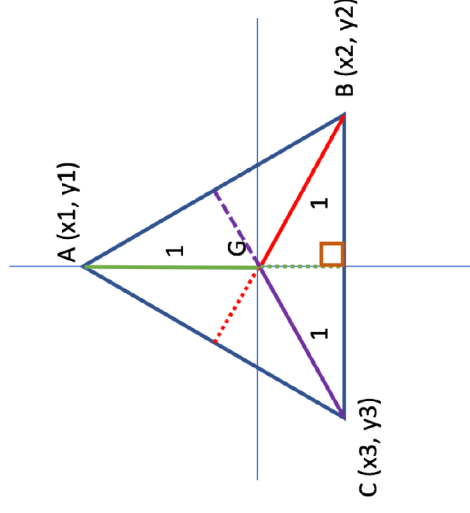


HOW TO TREAT THE SIGNALS

Schatz et. al. in prep



Centroid Equation for an equilateral triangle with the center at the origin



Slopes Map Equations

$$S_x = \frac{I_2 \left(\frac{\sqrt{3}}{2} \right) - I_3 \left(\frac{\sqrt{3}}{2} \right)}{I_1 + I_2 + I_3}$$

$$S_y = \frac{I_1 - I_2 \left(\frac{1}{2} \right) - I_3 \left(\frac{1}{2} \right)}{I_1 + I_2 + I_3}$$

4-sides

$$S_x = \frac{I_1 + I_2 - I_3 - I_4}{I_1 + I_2 + I_3 + I_4}$$

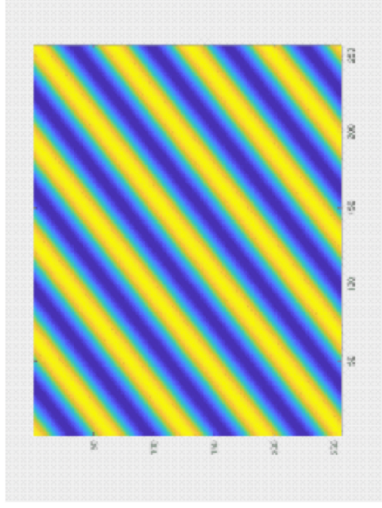
$$S_y = \frac{I_1 - I_2 - I_3 + I_4}{I_1 + I_2 + I_3 + I_4}$$

Or: Use the Full Frame Method

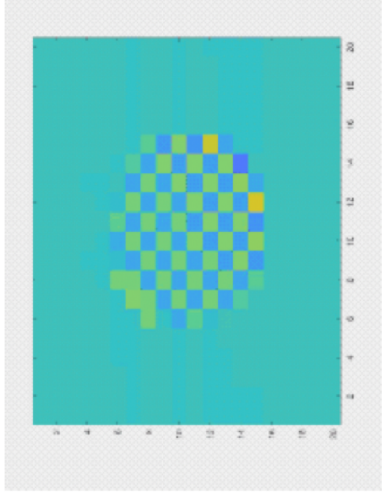
SENSITIVITY AS A FUNCTION OF SPATIAL FREQUENCY

Schatz et. al. in prep

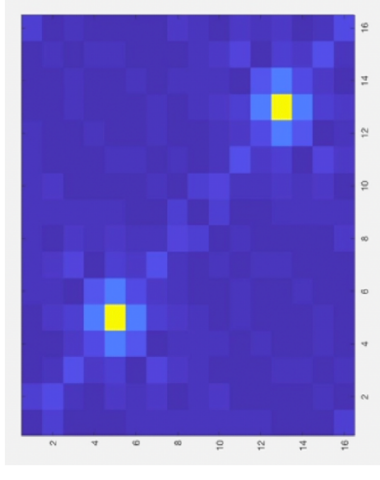
Input FM Mode



Compute slopes

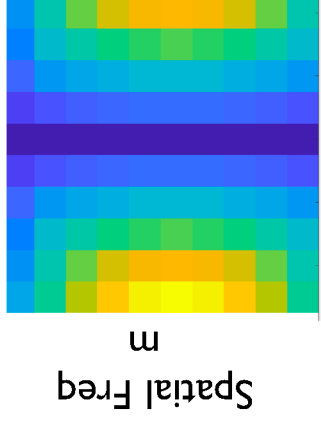


Fourier Transform



4

X-Direction



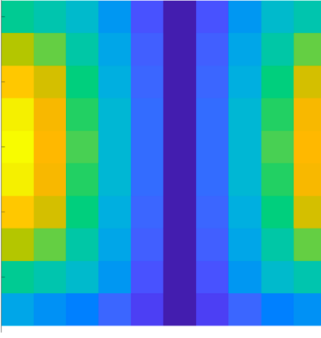
n

Spatial Freq

Spatial Freq

ϵ

Y-Direction



n

Spatial Freq

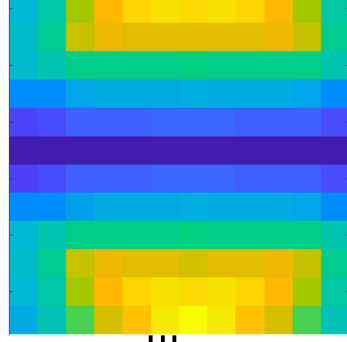
Spatial Freq

ϵ

5 λ/D modulation

3

X-Direction

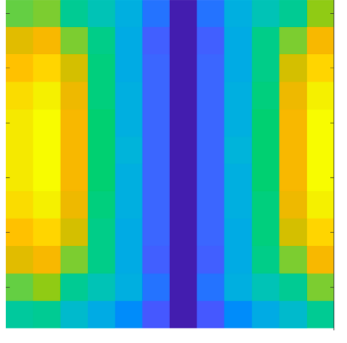


n

Spatial Freq

ϵ

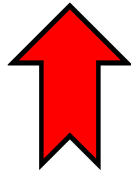
Y-Direction



n

Spatial Freq

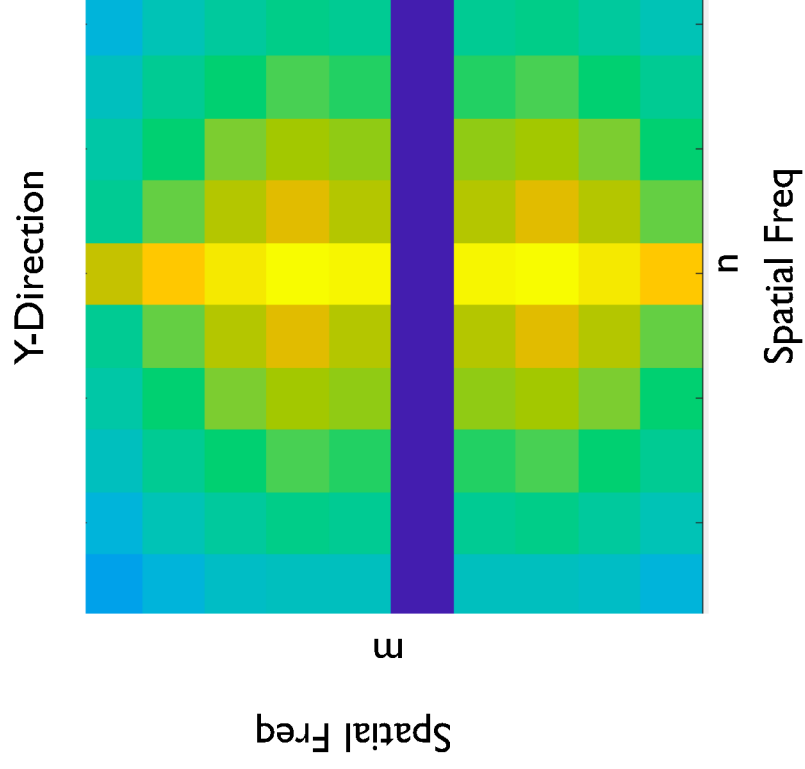
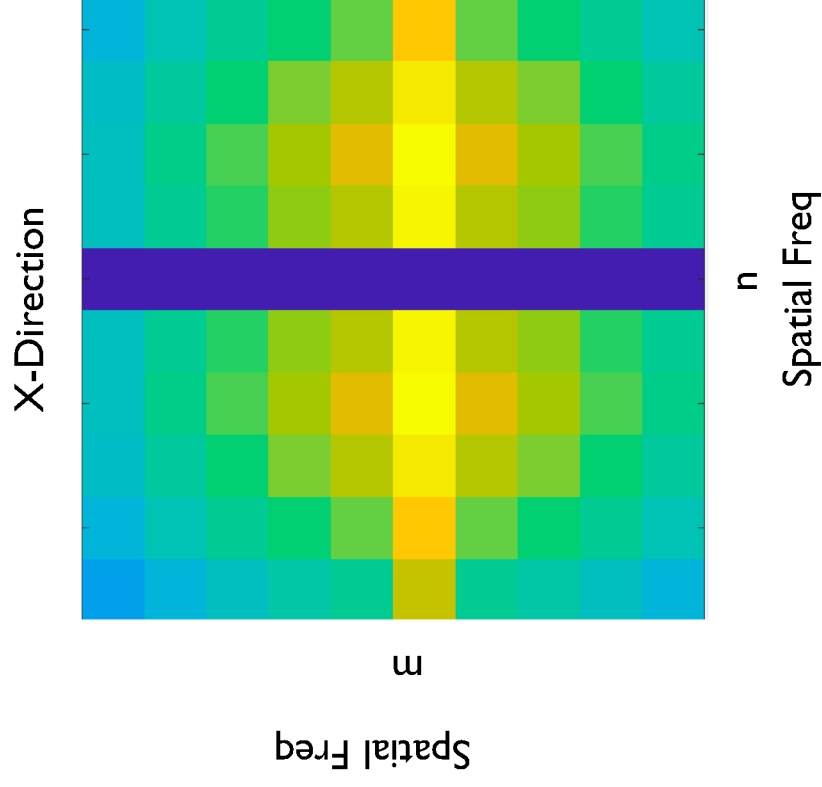
Result:
2D Fourier
Sensitivity
Map



Pyramid WFS

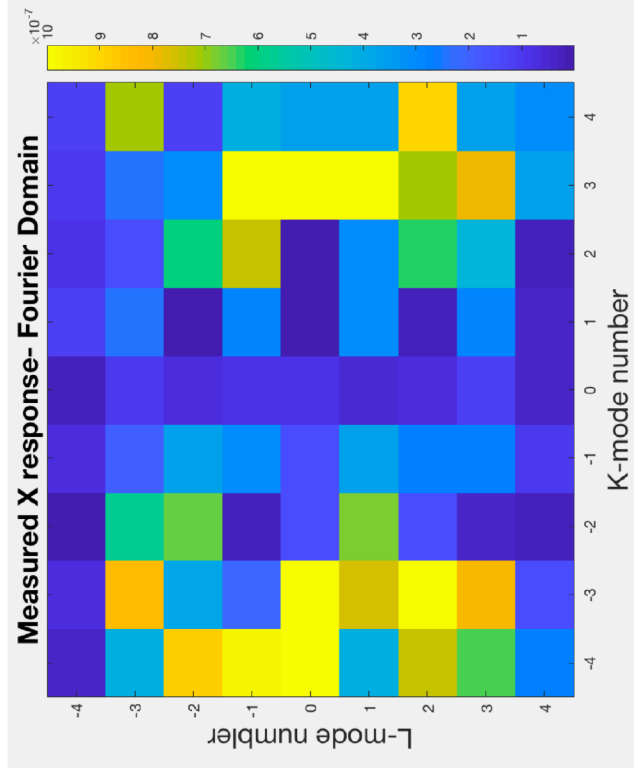
4PWFS NO MODULATION

Schatz et. al. in prep

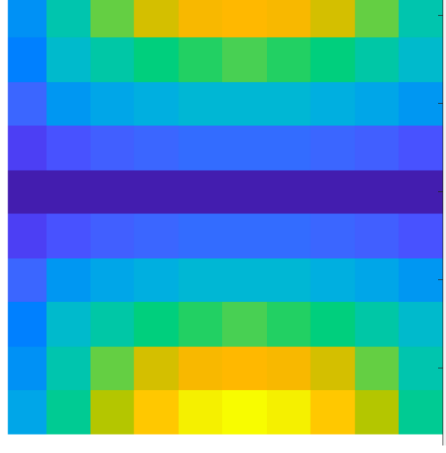


MEASURED RESULTS-Y

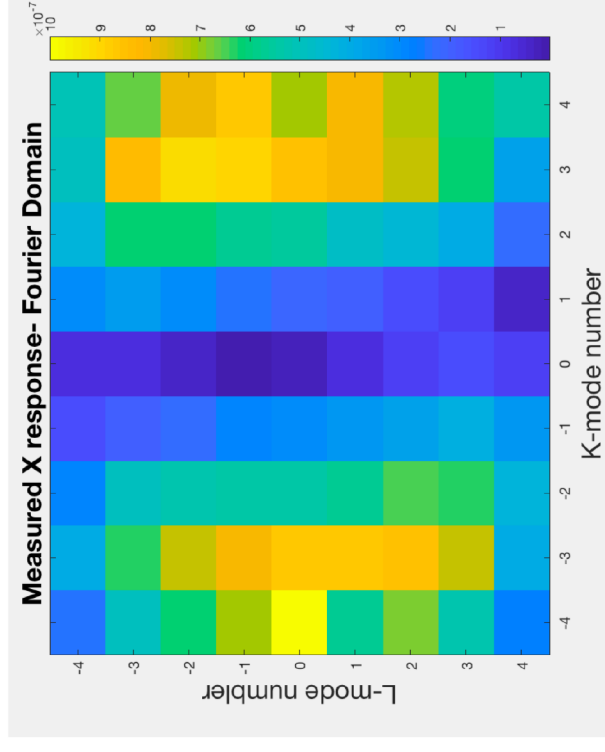
4PWFS



Simulated



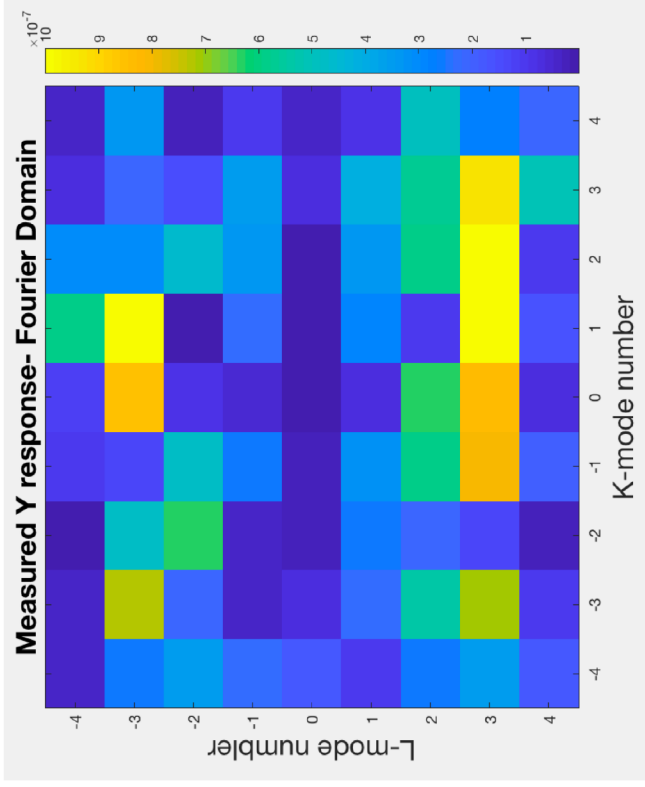
3PWFS



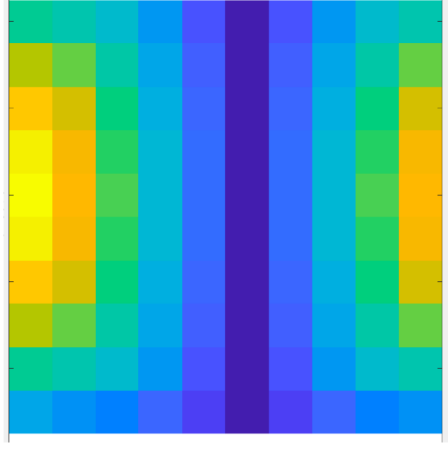
Normalized by Flux at each Spatial Frequency

MEASURED RESULTS-Y

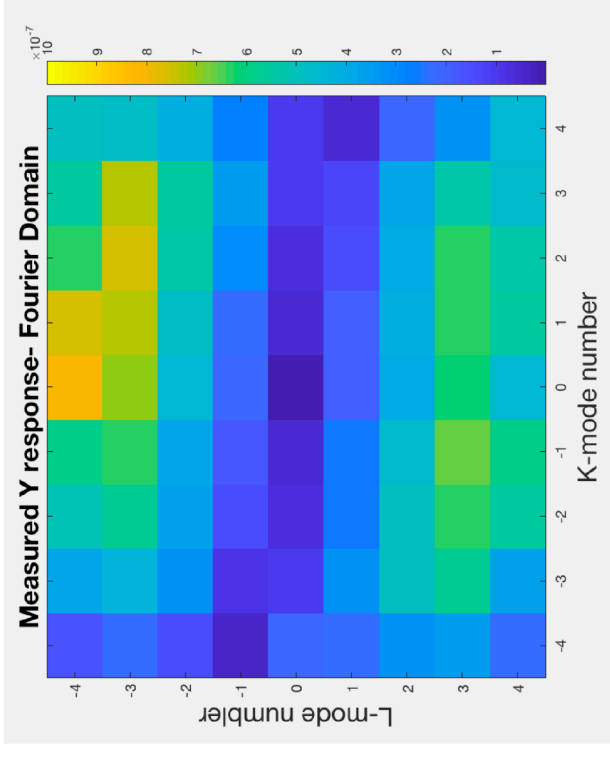
4PWFS



Simulated



3PWFS

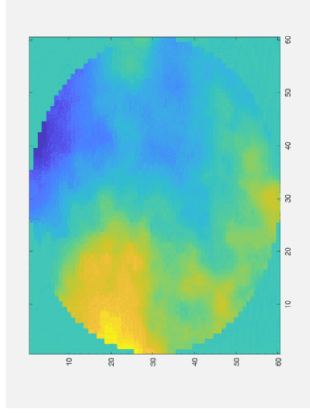


Normalized by Flux at each Spatial Frequency

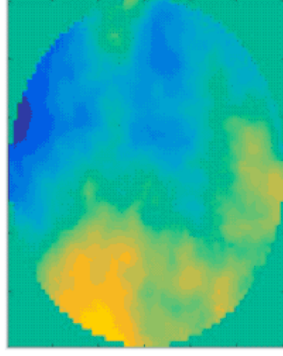
OVERALL PERFORMANCE

Schatz et. al. in prep

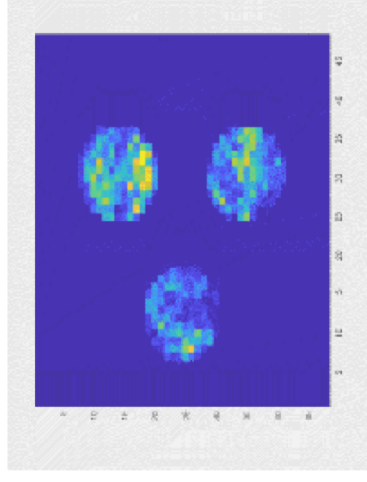
- End to end simulations done using OOMAO
- 2 m telescope
- $R_0=6\text{cm}$
- 1 phase screen moving at 7.4 m/s
- 8 DM actuators
- 20 pixels across each pupil



Input phase screen

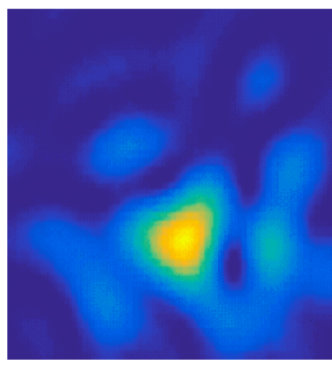


Residual phase



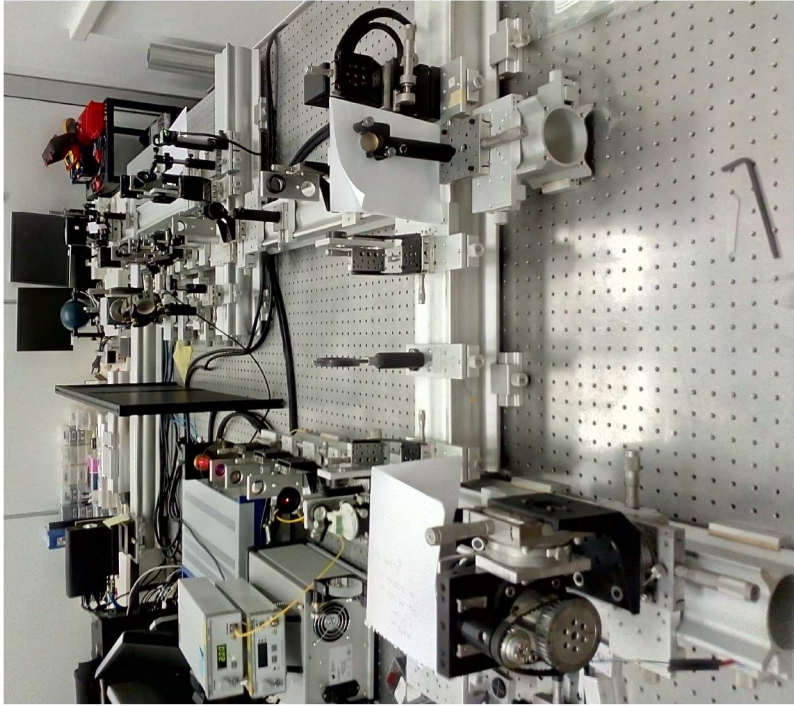
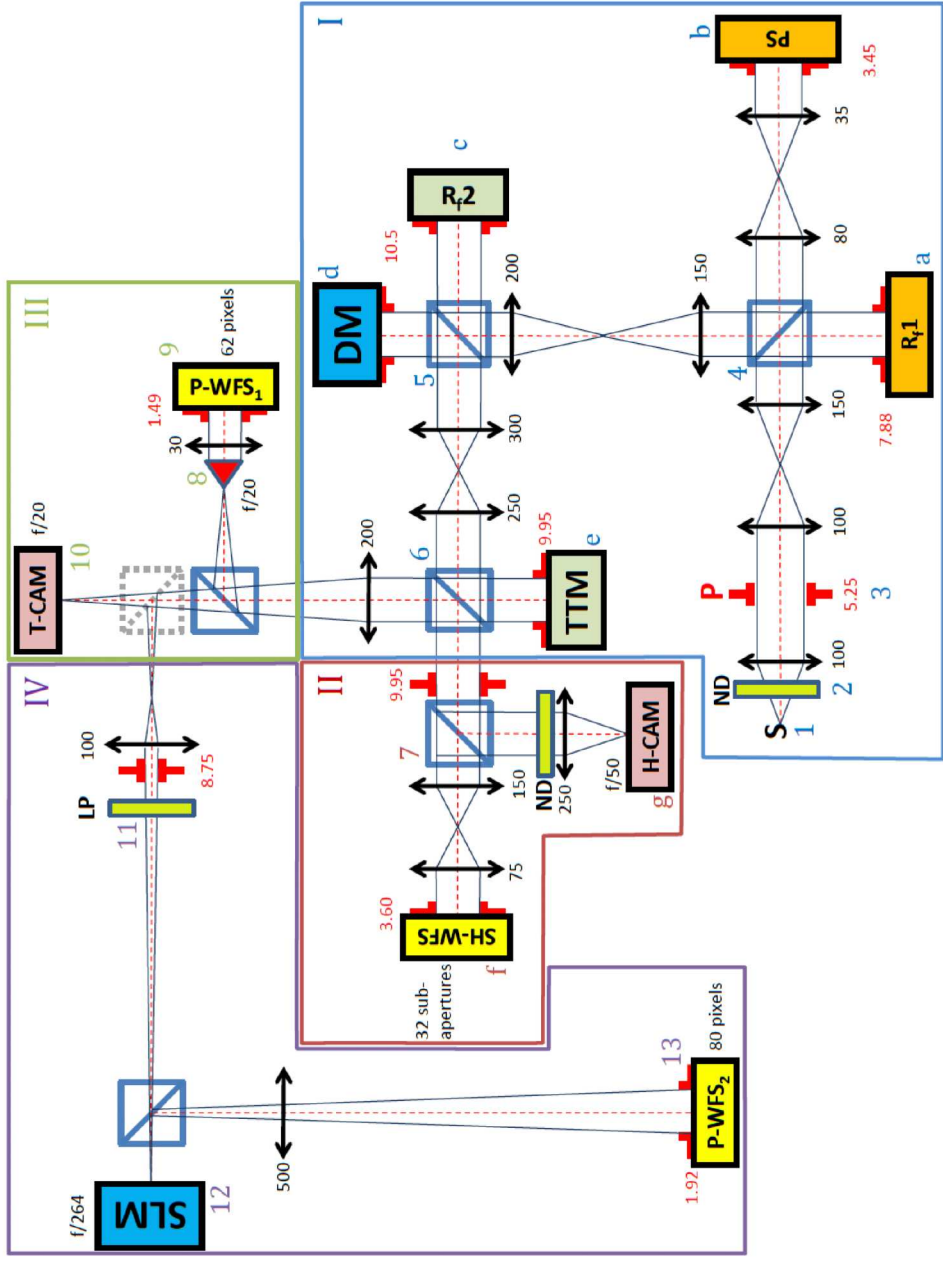
WFS camera

$5 \frac{\lambda}{D}$ modulation



PSF

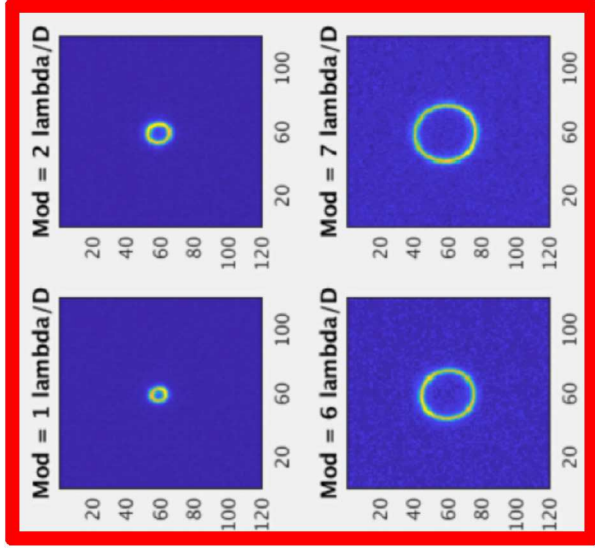
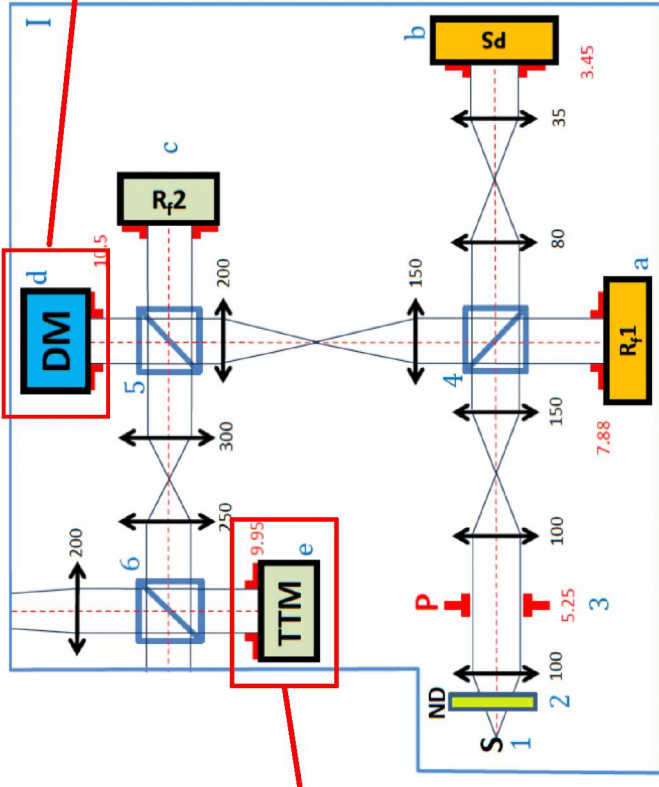
Pyramid WFS



Pyramid WFS



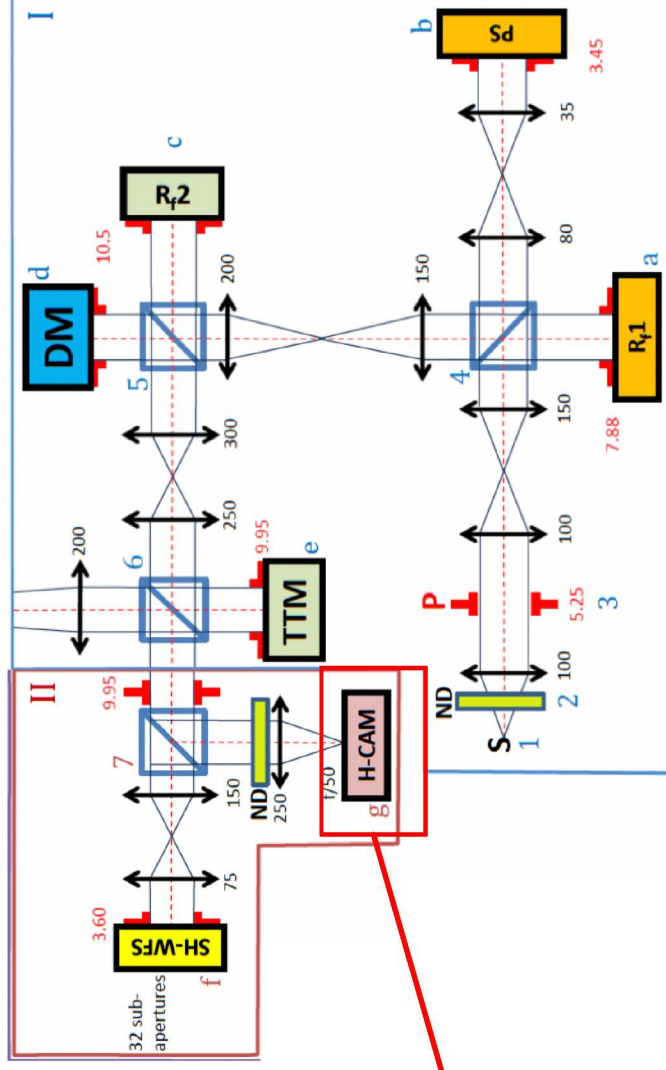
- Fiber Source
- Reflective Phase Wheel
- Alpao69
- Modulation Stage





- 32x32 Shack Hartmann
- Hamamatsu ORCA-Flash CMOS science camera

Can Measure Strehl



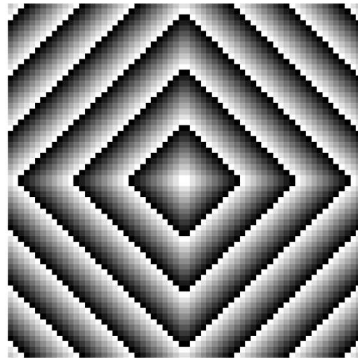
Pyramid WFS



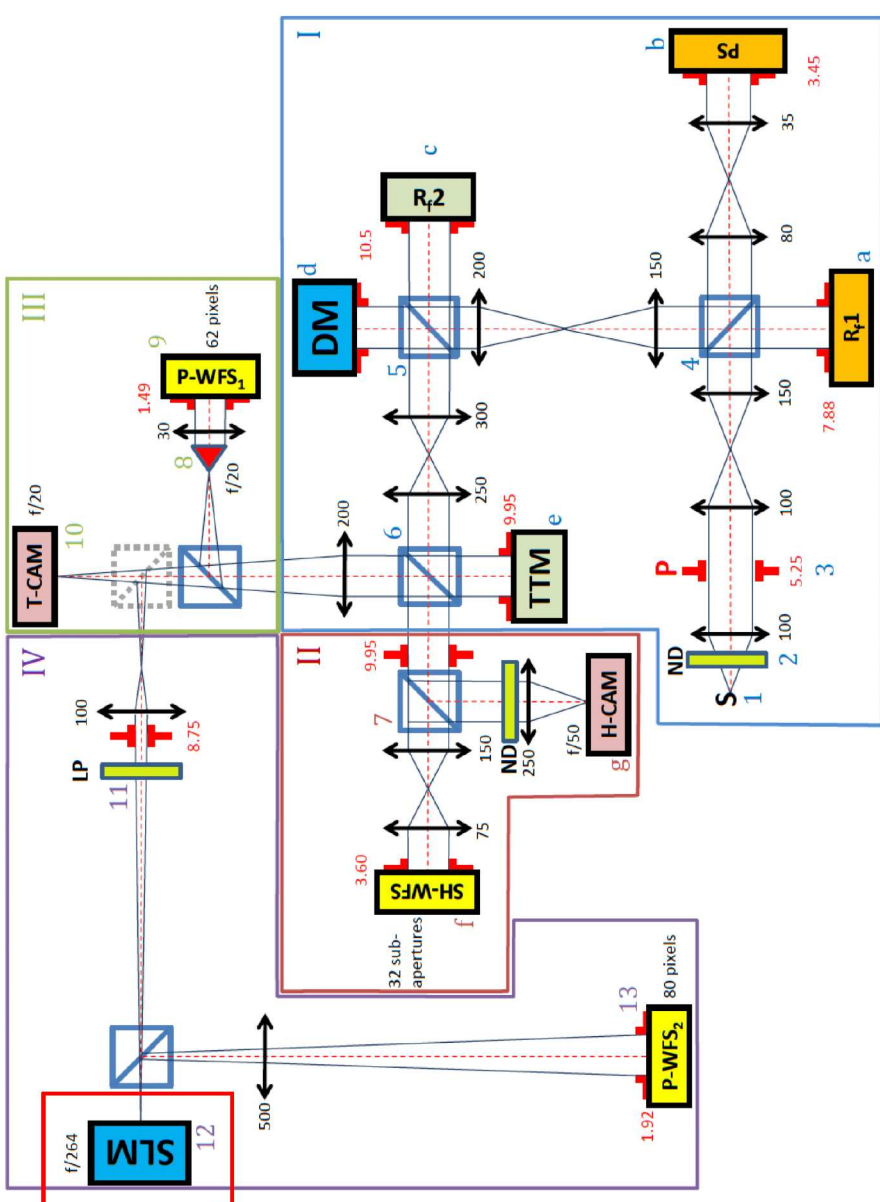
Place in Focal Plane



Spatial Light Modulator

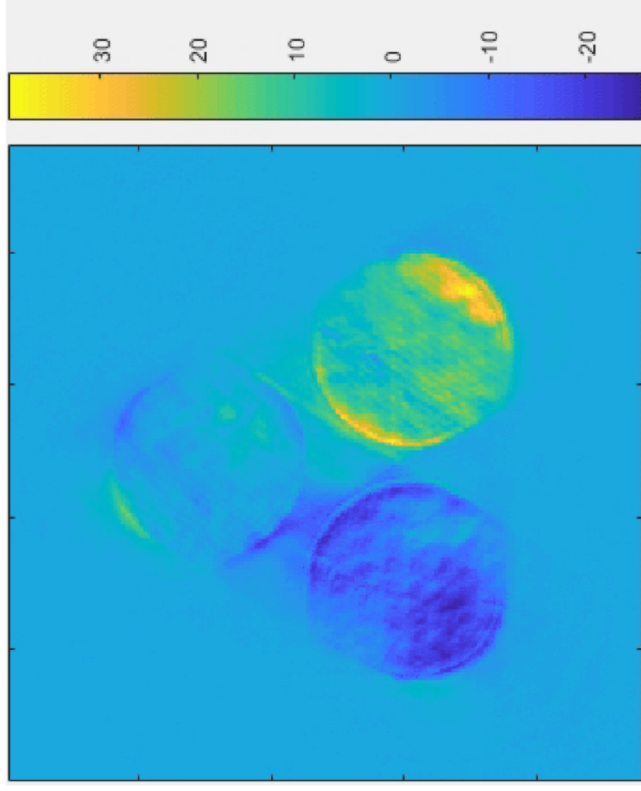


Phase mask

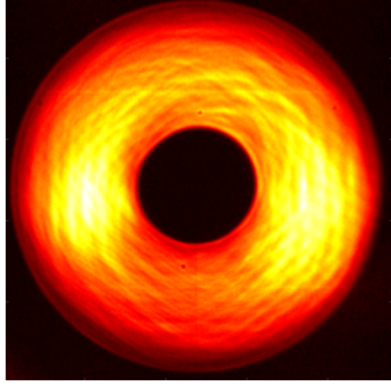


NEW WAVEFRONT SENSORS ON LOOPS

3PWFS



Axicone



Flattened

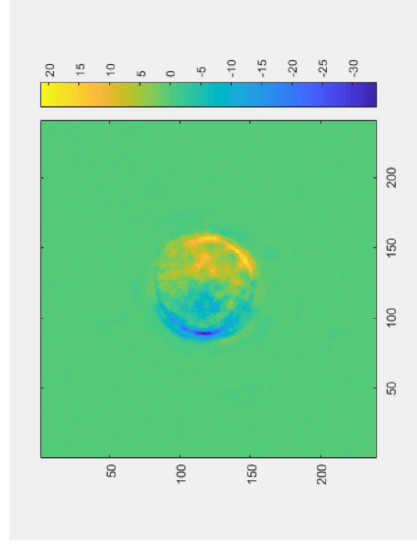
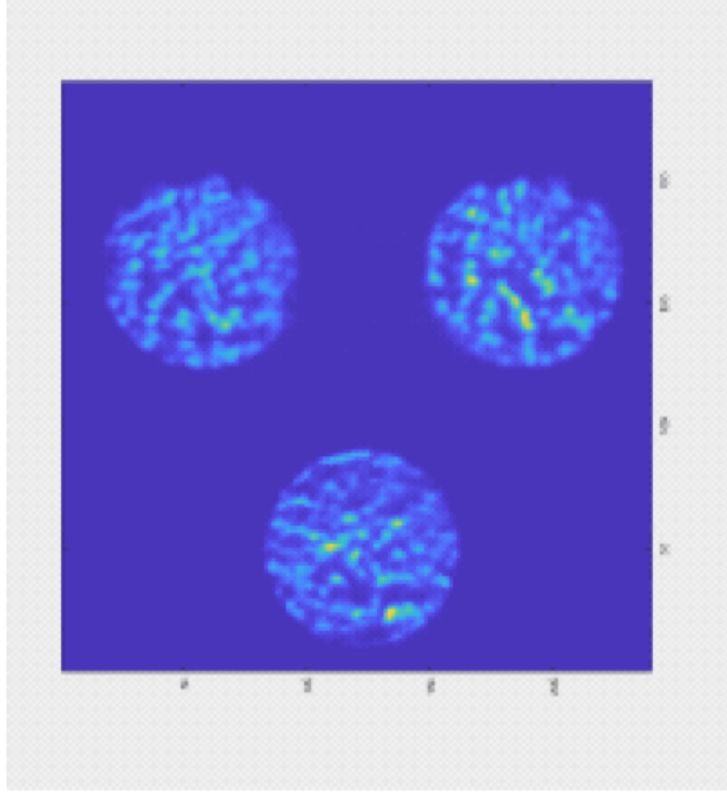
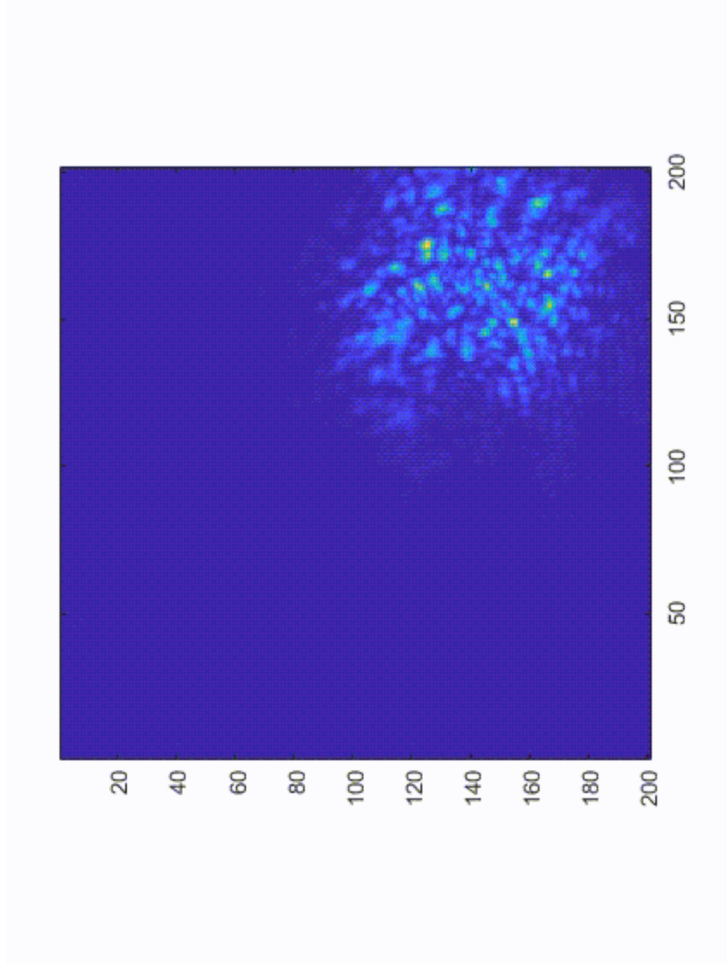


Photo: Credit Pierre Janin-Potiron

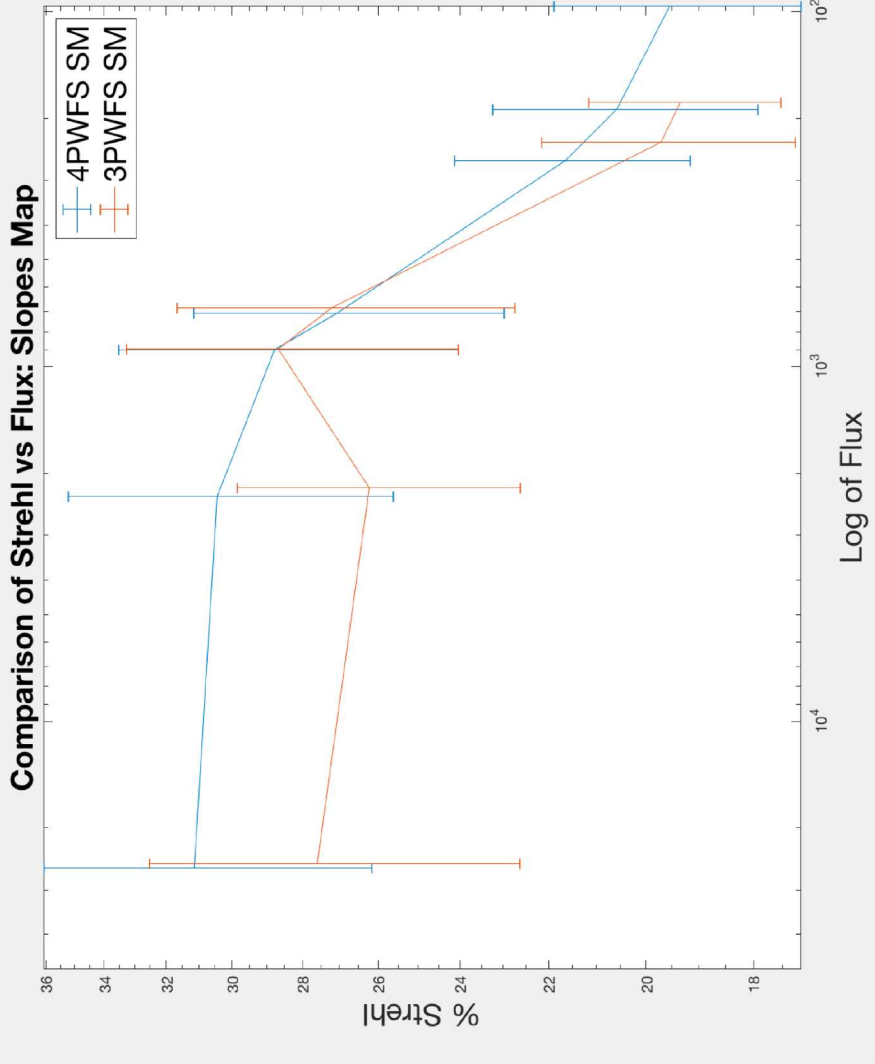
FIRST MILESTONE: CLOSED LOOP ON THE 3PWFS!!



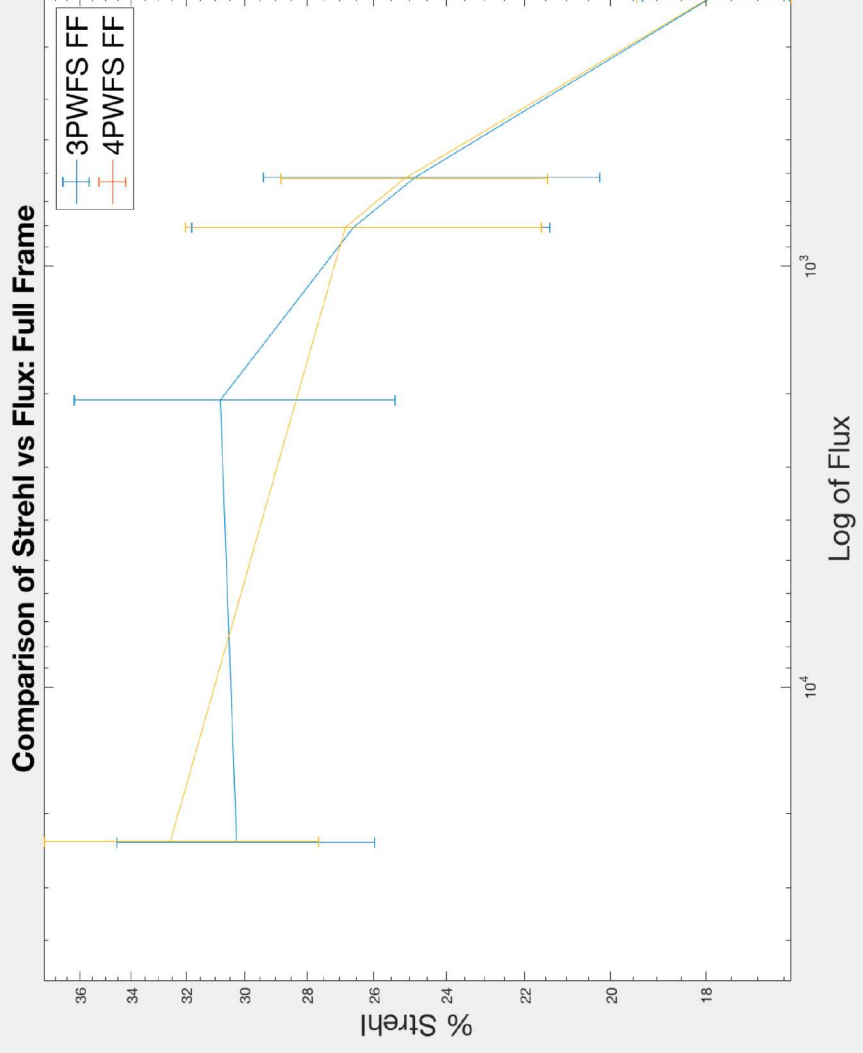
END TO END PERFORMANCE EXPERIMENTAL DETAILS

- Closed Loop at different levels of flux on the OCAM
 - Used a ND filter wheel to vary light
- Tried different Reconstructor: Full Frame, Slopes Maps
- At each step:
 - Took ~3 minutes of Shack Hartmann Data
 - Mean RMS Residual Wavefront
 - Zernike Decomposition of the Residual Wavefront
 - Took 2048 images of the PSF on the Hamamatsu
 - Calculated Strehl for each image, took the mean value.
 - Recorded the Flux on the detector from an average of 2000 frames, only considered light in the pupils. (Used a flat wave front, no turbulence.)

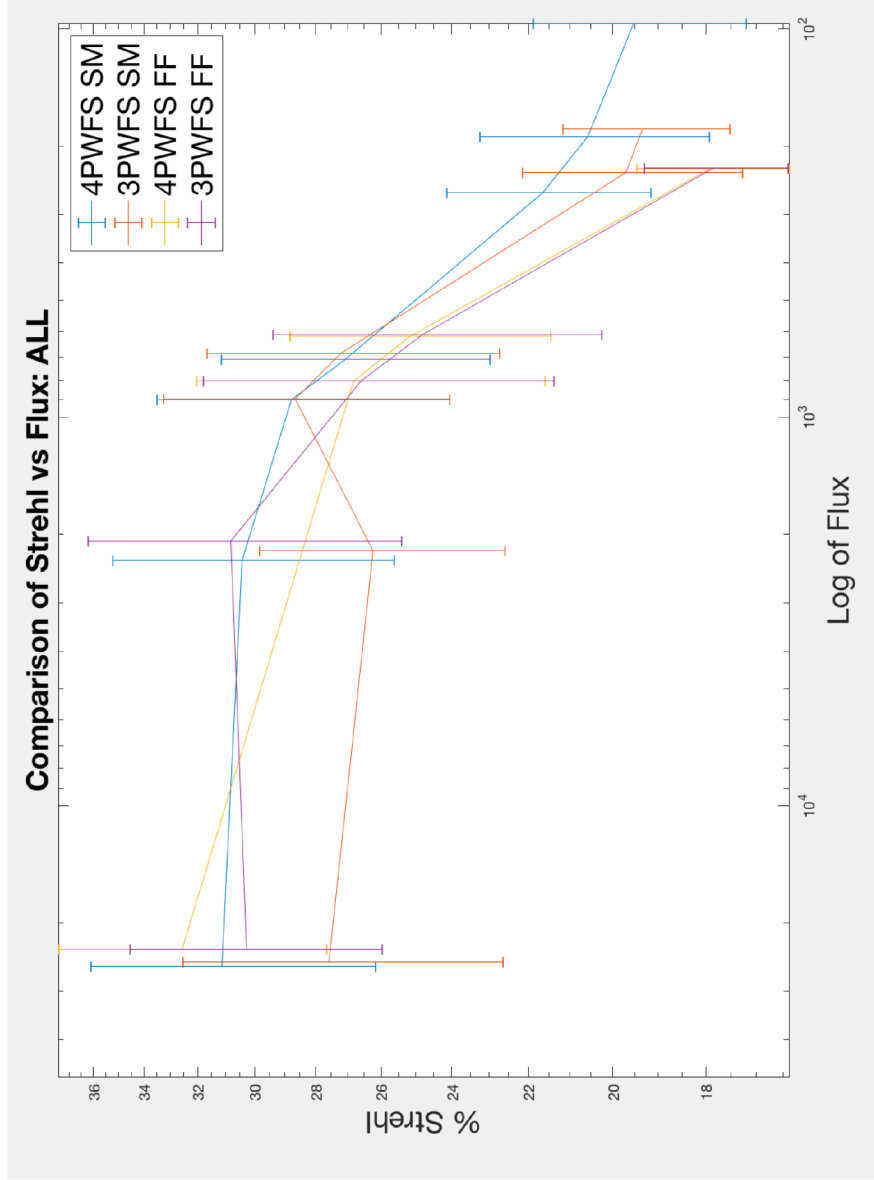
STREHL VS FLUX SLOPES MAPS



STREHL VS FLUX FULL FRAME



STREHL COMPARISON: AND FINAL CONCLUSIONS



Based on Mean: Full
Frame is better

Performance of the Full
Frame 3PWFS vs 4PWFS
very similar

- Error bars high- need to take more data

SPECIAL THANKS

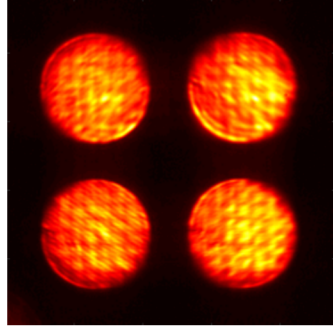
My Team Here: Benoit Neichel, Thierry Fusco, Carlos Correia, Pierre Janin-Patiron, Vincent Chambouleyron, Olivier Fauvarque

My Friends I have made here: Jana, Jorge, Sean, Elodie ... the list goes on

My advisor Jared Males for being cool with letting me come here

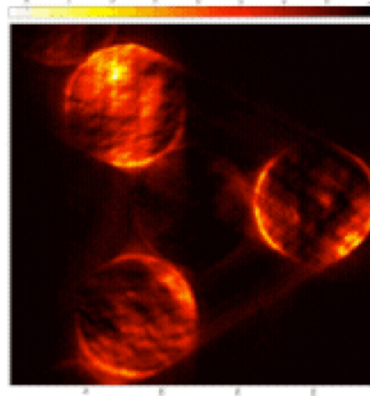


4PVFS



3PVFS

Real time on the SLM!



Axicone

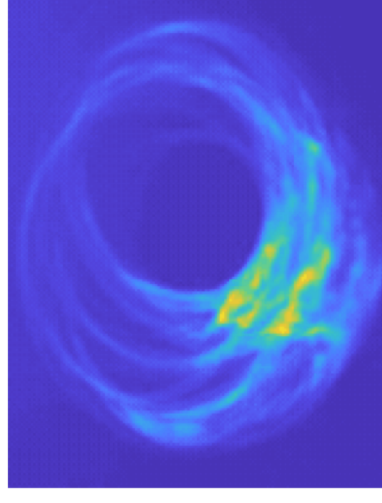
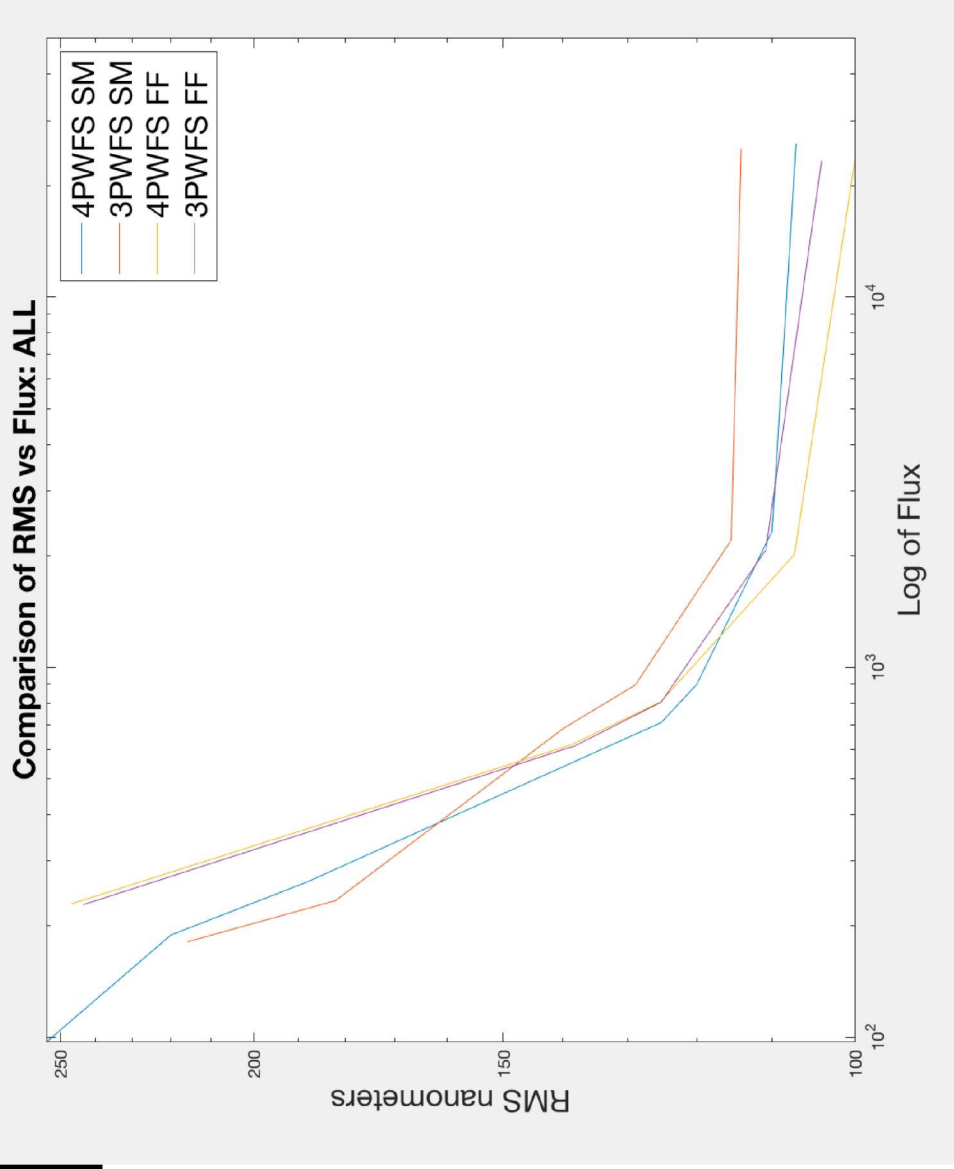


Photo: Credit Pierre Janin-Potiron

CANNED SLIDES

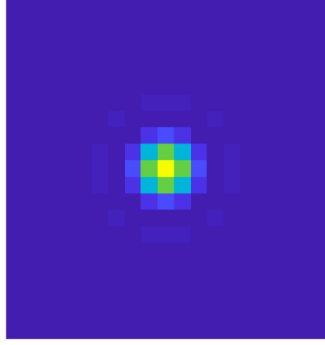


RMS VS FLUX

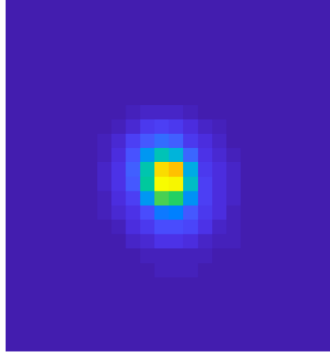


END TO END TESTS: 4PWFS

Perfect Simulated

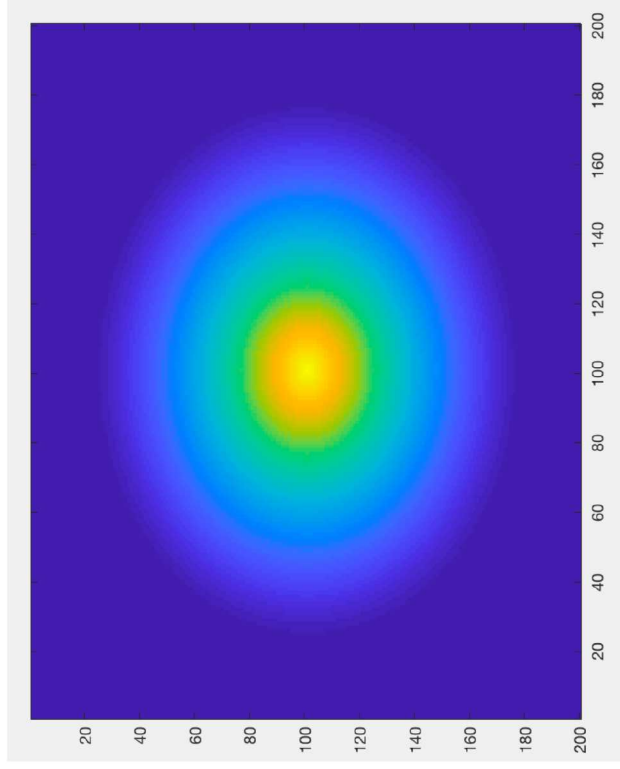


Perfect Bench

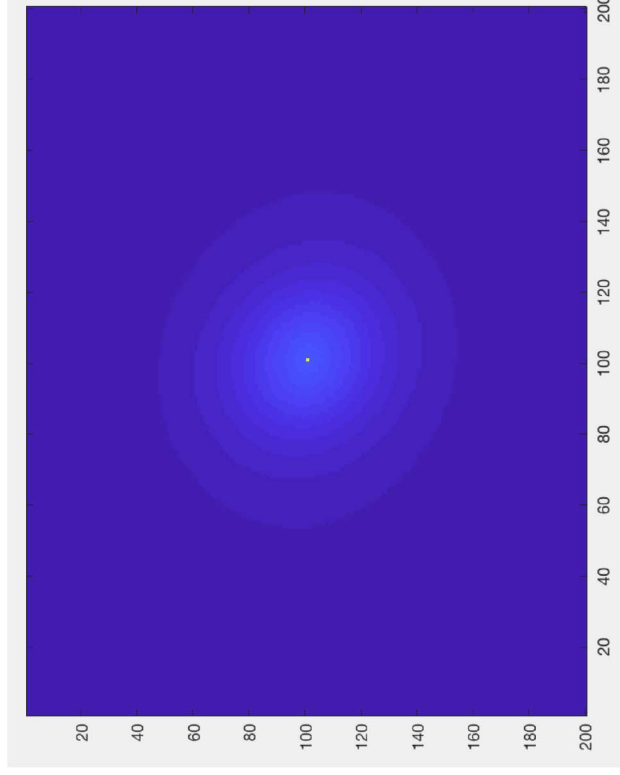


OTFS

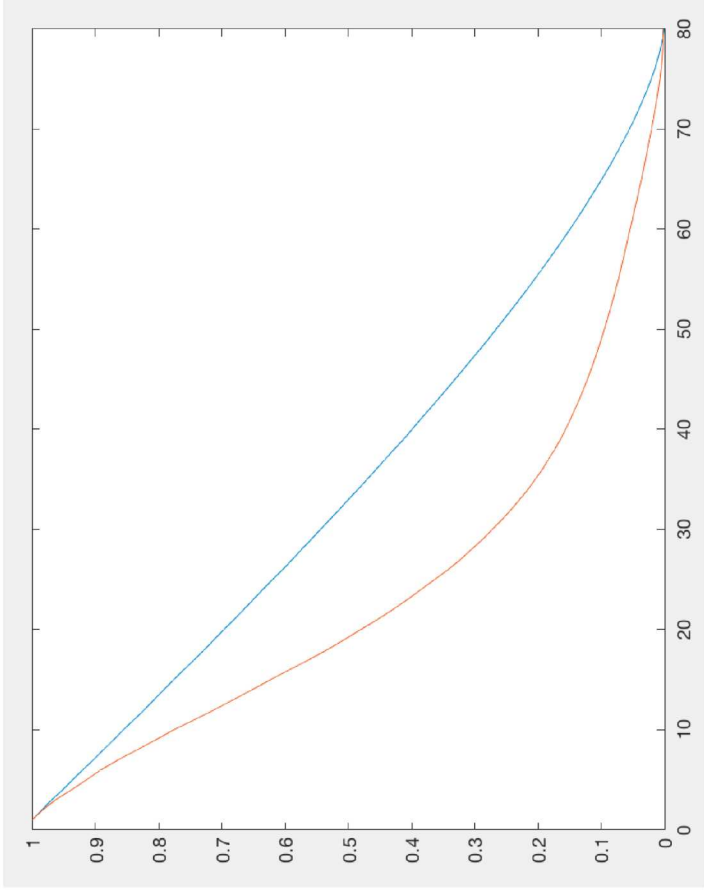
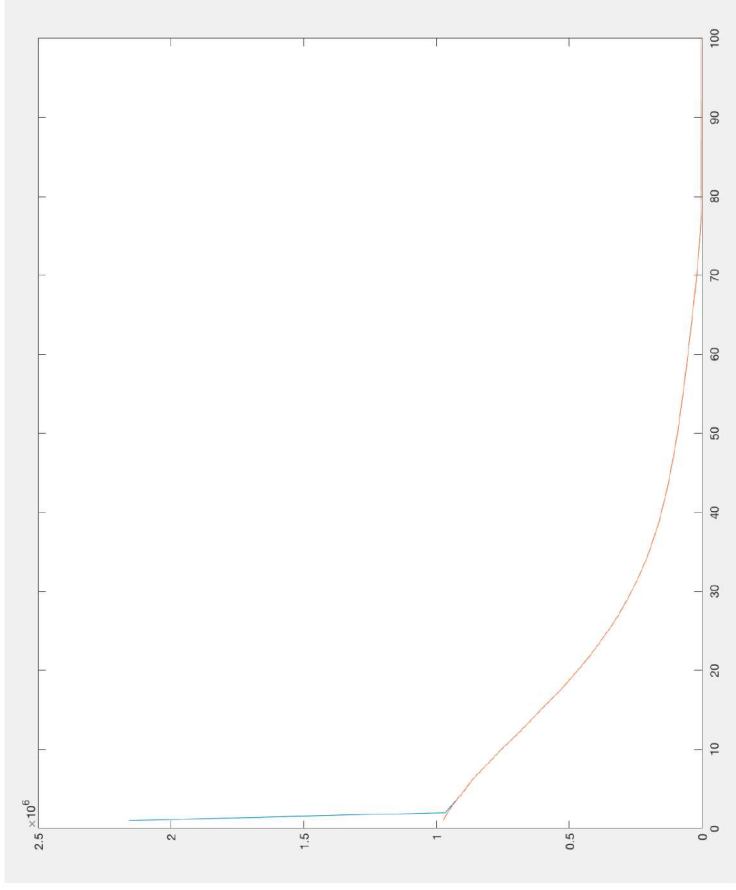
Perfect Simulated



Perfect Bench OTF

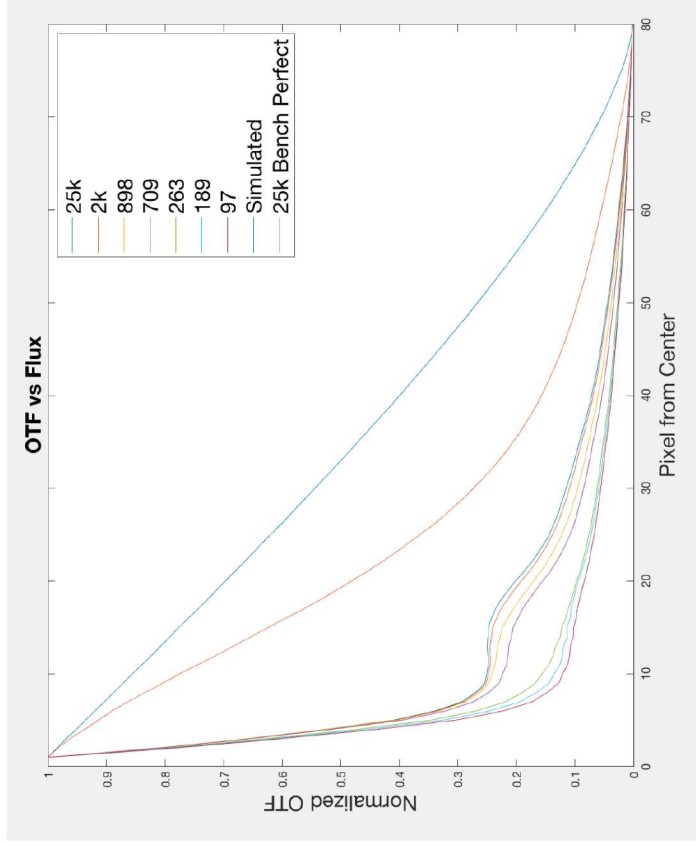


OTF FITTING

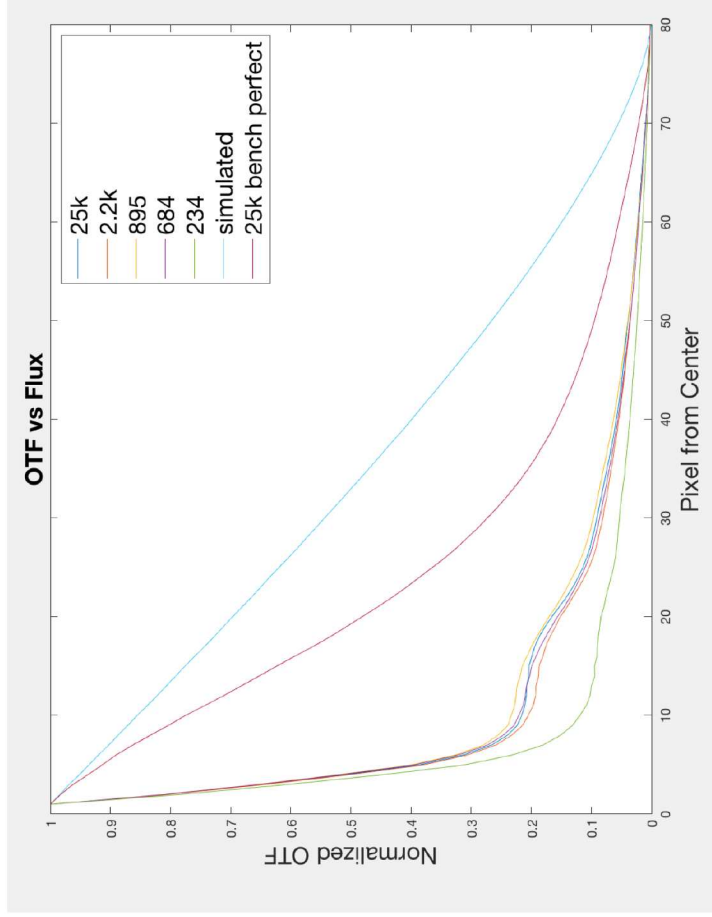


RESULTS: SLOPES MAPS

4PWFS

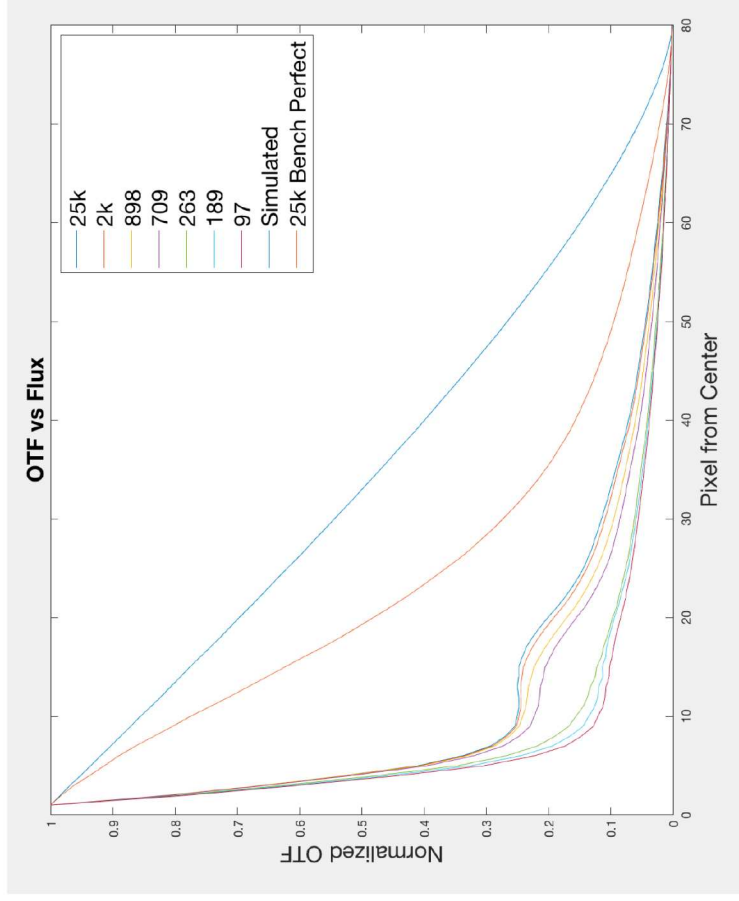


3PWFS

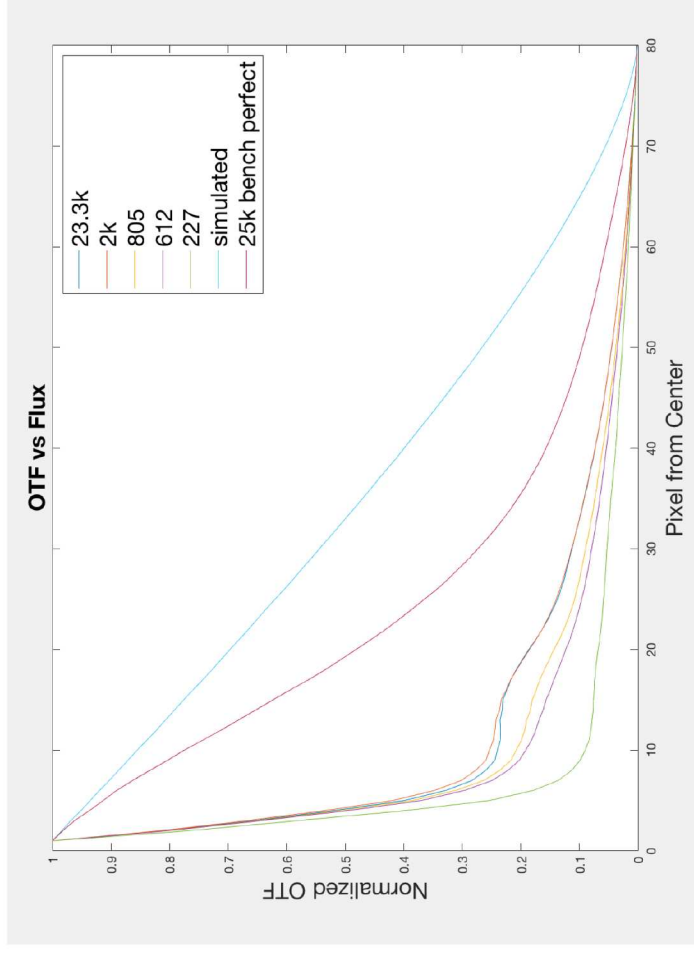


RESULTS: FULL FRAME

4PWFS



3PWFS

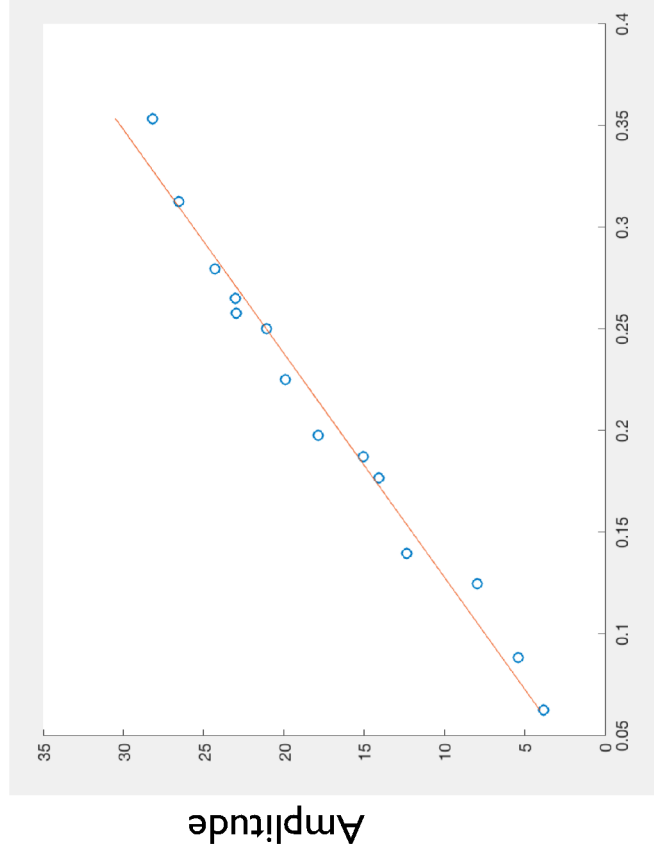


MATHEMATICS OF WAVEFRONT SENSORS

- Derivative wavefront sensor: Linear with spatial frequency

- $\phi(k) \propto A \sin(kx)$
- $\frac{d}{dx} \phi(k) \propto Ak \cos(kx)$

Shows the linear relation of the SH to K



Spatial Frequency

4PWFS

Shift from measurement point (CCD pixel)
to reconstruction point (actuator)

Pixel averaging
(discrete process)

Flat response

$$\tilde{G}(\kappa) = e^{i\pi d(\kappa_x + \kappa_y)} \text{sinc}(d\kappa_x) \text{sinc}(d\kappa_y) \left\{ \begin{array}{l} \text{Flat response} \\ i \frac{\text{sgn}(\kappa)}{2j} \frac{\sin\left(\frac{\kappa}{\kappa_{\text{mod}}}\right)}{\pi} \end{array} \right\}$$

Modulated response

$$|\kappa| > \kappa_{\text{mod}}$$

$$|\kappa| \leq \kappa_{\text{mod}}$$

Credit: Charlotte Bond

